

# ICORE : Innovative COating REsearch

*Innocenzo M. Pinto*

University of Sannio, INFN, LVC and KAGRA



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*Rome, IT, March 2, 2016*

# Outlook

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## Why Coating R&D

Where are we now : the aLIGO mirrors

How can we progress:

- Improving Modeling
- Improving Processes
- Improving Characterization

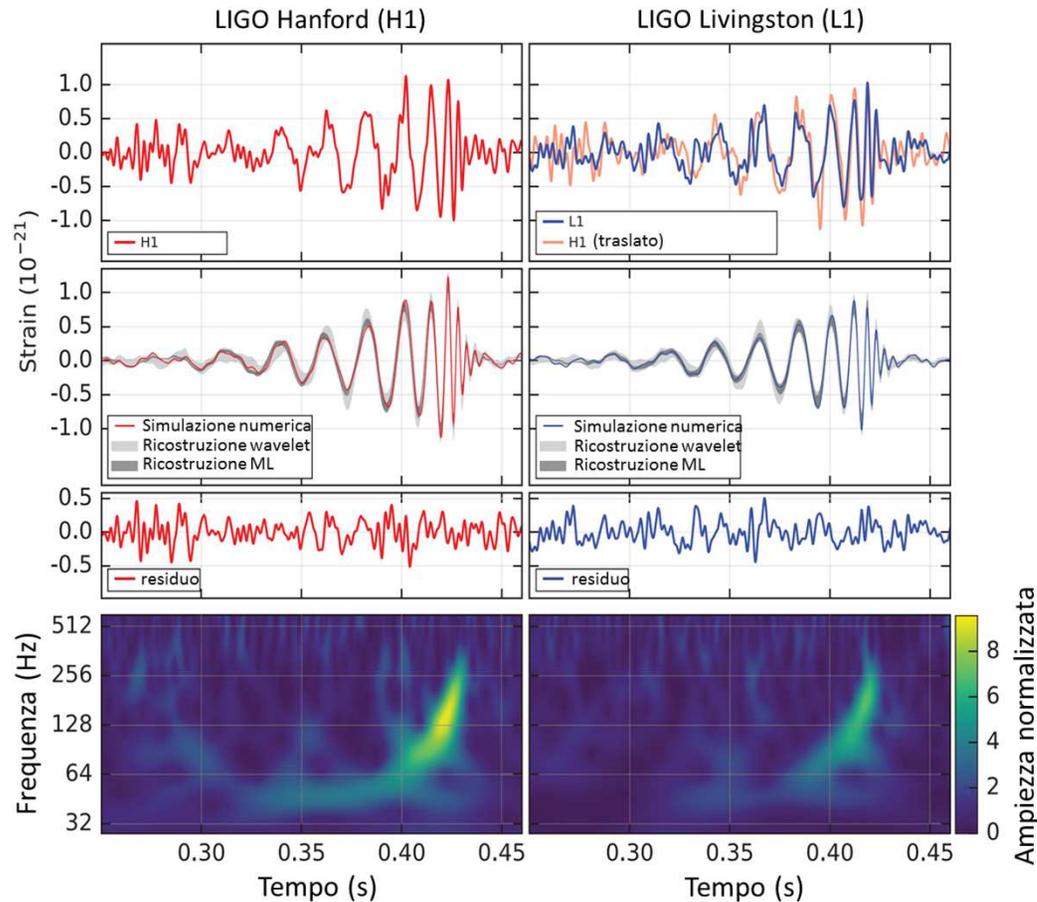
Ongoing Studies & New Ideas:

- Nanolayered Composites
- Silicon Nitrides
- Crystalline Coatings
- M-ary Coatings
- Metamaterial Coatings

Conclusions

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# GW150914, 1<sup>st</sup> Detected GW



	Valore stimato	Unitá
$M_1$	$36^{+5}_{-4}$	$M_\odot$
$M_2$	$29^{+4}_{-4}$	$M_\odot$
$M_{\text{fin}}$	$62^{+4}_{-4}$	$M_\odot$
$s$	$0.67^{+0.05}_{-0.07}$	-
$R_L$	$410^{+160}_{-180}$	$Mpc$
$Z$	$0.09^{+0.03}_{-0.04}$	-

# Expected Pay-offs : Astrophysics

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Observation of GW from extreme – mass – ratio - inspirals (EMRI) allows mapping the spacetime geometry [J.R. Gair et Al., Phys. Rev. D77 (2008) 024035] around a collapsed galactic core (*holiodesy*)

Gravitational radiation from spinning neutron stars (pulsars), and neutron-star binaries in their merger phase will bring signatures of the equation of state of nuclear star matter [J. S. Read et al., Phys.Rev. D79 (2009) 124033], and indicate whether strange (quark) particles or exotic phase transitions are involved;

Reconstructing the mass multipoles of the collapsed cores from the observed waveforms, it will be possible to check the black hole “no-hair” theorem [L. Barack and C. Cutler, Phys. Rev. D75 (2007) 042003]

Compact binary systems in their inspiral (pre-coalescence) phase are standard candles of gravitational light, whose observation will permit to measure Hubble’s recession to an unprecedented degree of accuracy [S. Capozziello, Astroparticle Physics, 33 (2010) 190]

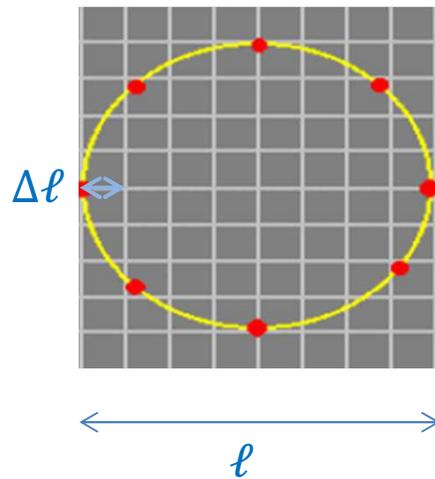
# The *Big Ears* (as of 2017)

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# Interferometric Detectors

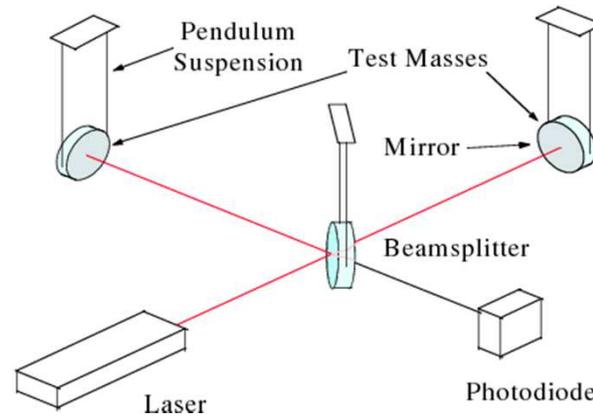
Effect of monochromatic GW  
(+ polarization, normal incidence)  
on a planar ring of freely-falling  
test particles



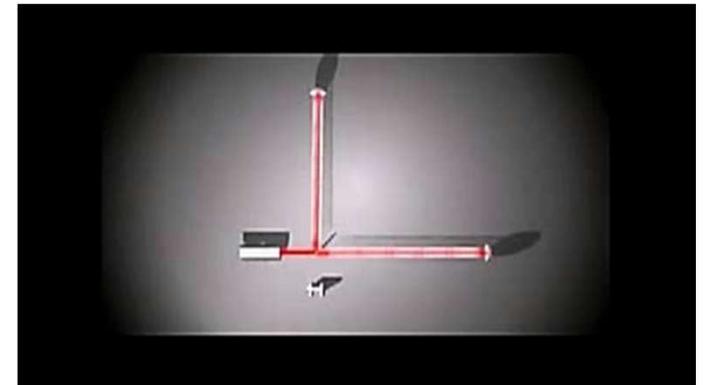
Tidal force:  $\Delta\ell \propto \ell$

Typical wave strength :  $h \cong \Delta\ell / \ell \approx 10^{-26} \div 10^{-19}$  - **Very weak !!!**

Incoming GW

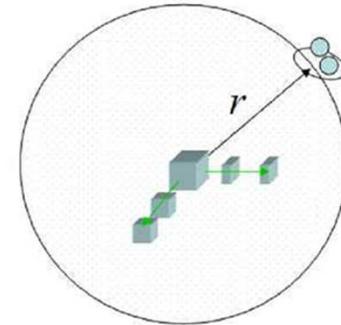
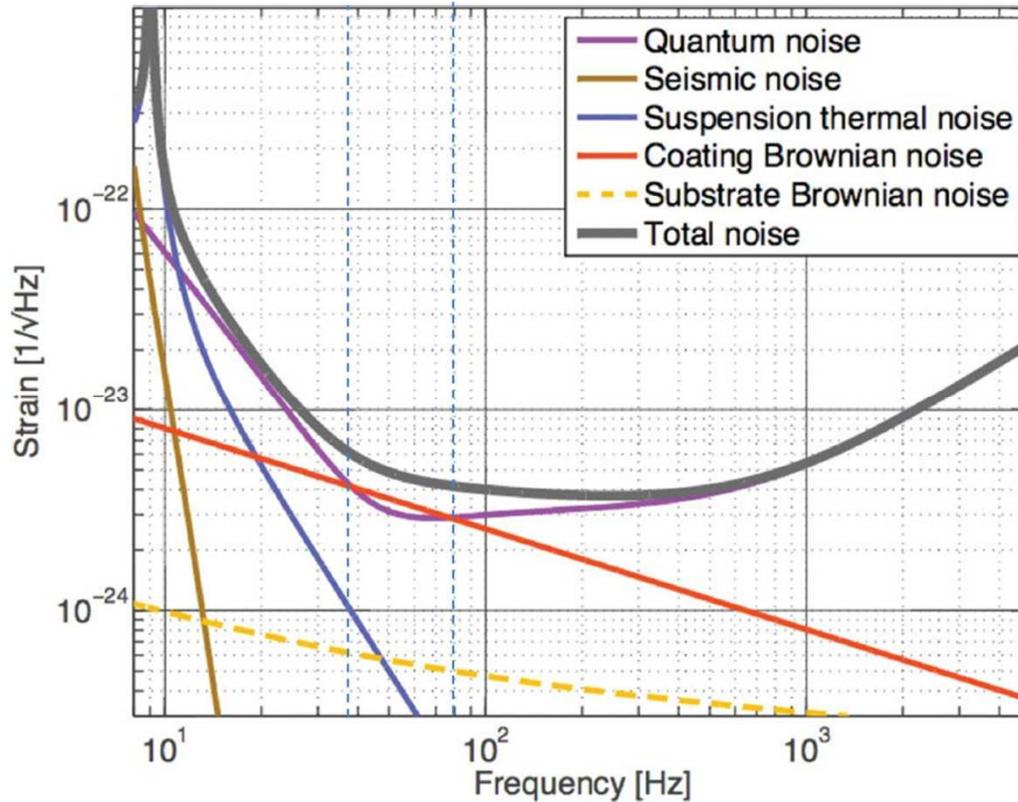


A bare-bone interferometric  
detector of GW



... transforms the GW into an  
electric signal (antenna = transducer)

# aLIGO Noise Budget



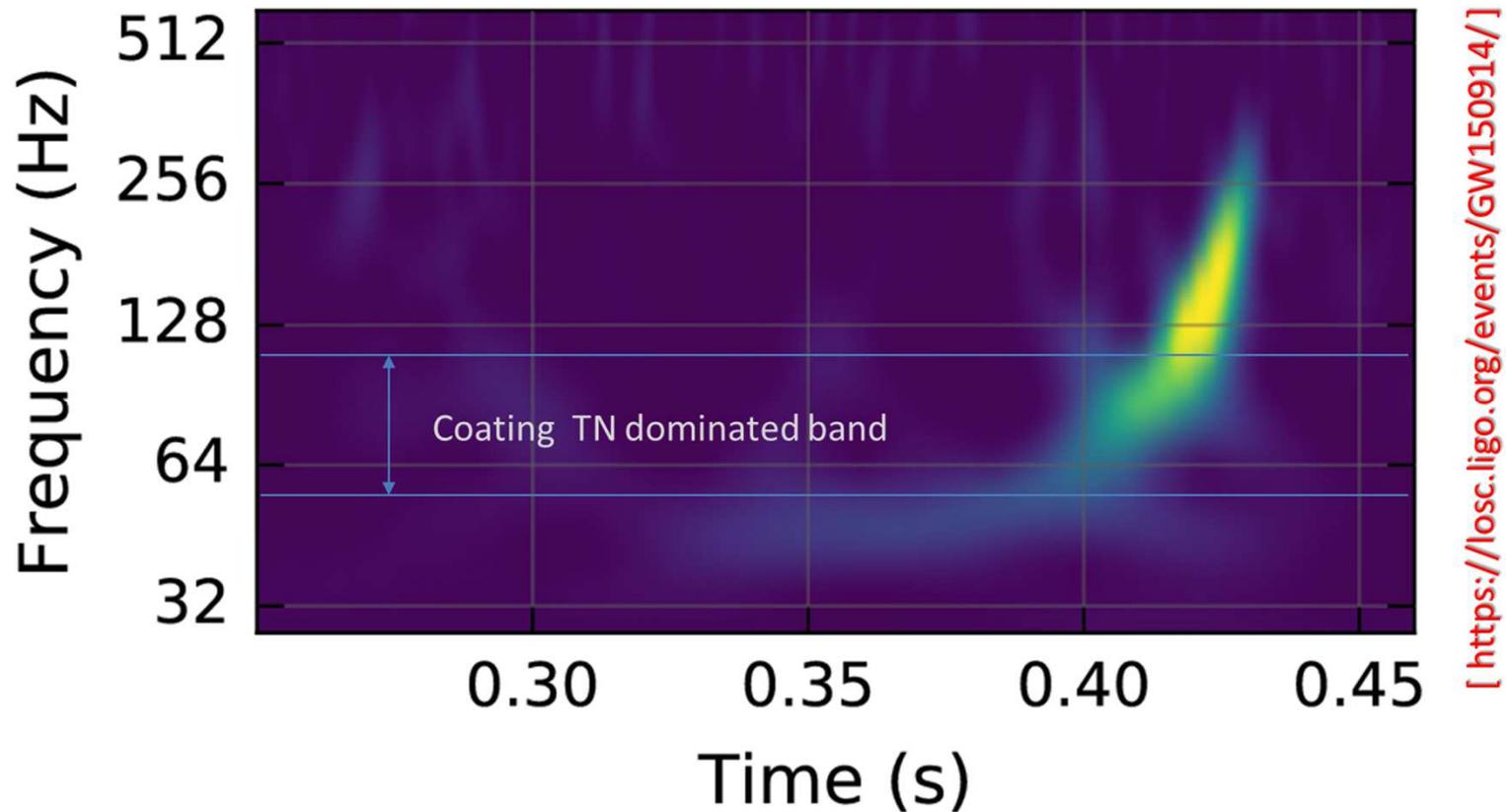
Visibility volume & event rate }  $\propto PSD_{floor}^{-3/2}$

... a **5 $\mu$ m** thick film sets the performance of a **5Km** size detector !!

[Waldman, LIGO P0900115]

# GW150914, 1<sup>st</sup> Detected GW

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# Coating R&D Funding

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At the 1<sup>st</sup> “post detection” LVC Meeting in March 2016, the NSF representatives solicited the LIGO coating working groups to submit a cooperative R&D on the subject, *worth 3M US\$ on a 3y span*.

On July 7-8 2016 at the 2nd Dawn Workshop, hosted by Georgia Tech, a focus Session on coating R&D was held, where the proposal guidelines and the collaboration structure were set.

The final version of the proposal was completed on Dec. 16 2016.

There's no EGO-Virgo counterpart, as yet.



# Coating R&D Funding in Italy

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Coating R&D funding on behalf of Italian Research Agencies:

INFN COAT (Pinto et al.)

INFN MiDiBRUT (Pinto et al.)

MURST/MIUR COACH (Vetrano et al.)

INFN AdCOAT (Pinto et al.)

... worth *a few* tens KEUR total ...



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- Improving Characterization

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- Silicon Nitrides
- Crystalline Coatings
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- Metamaterial Coatings

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# Basic Coating Noise Formula

$$S_{coat}^{(B)}(f) = \frac{2k_B T}{\sqrt{\pi^3} f} \frac{1 - \sigma^2}{w_m Y} \phi_c$$

Temperature →  $2k_B T$

Coating loss angle (mechanical, F/D theorem) →  $1 - \sigma^2$

Beam spot-size →  $w_m Y$

$$\phi_c = \frac{\lambda_0}{w \sqrt{\pi}} (\eta_L d_L + \eta_H d_H), \quad \eta_{L,H} = \frac{\phi_{L,H}}{n_{L,H}} \left( \frac{Y_{L,H}}{Y_s} + \frac{Y_s}{Y_{L,H}} \right)$$

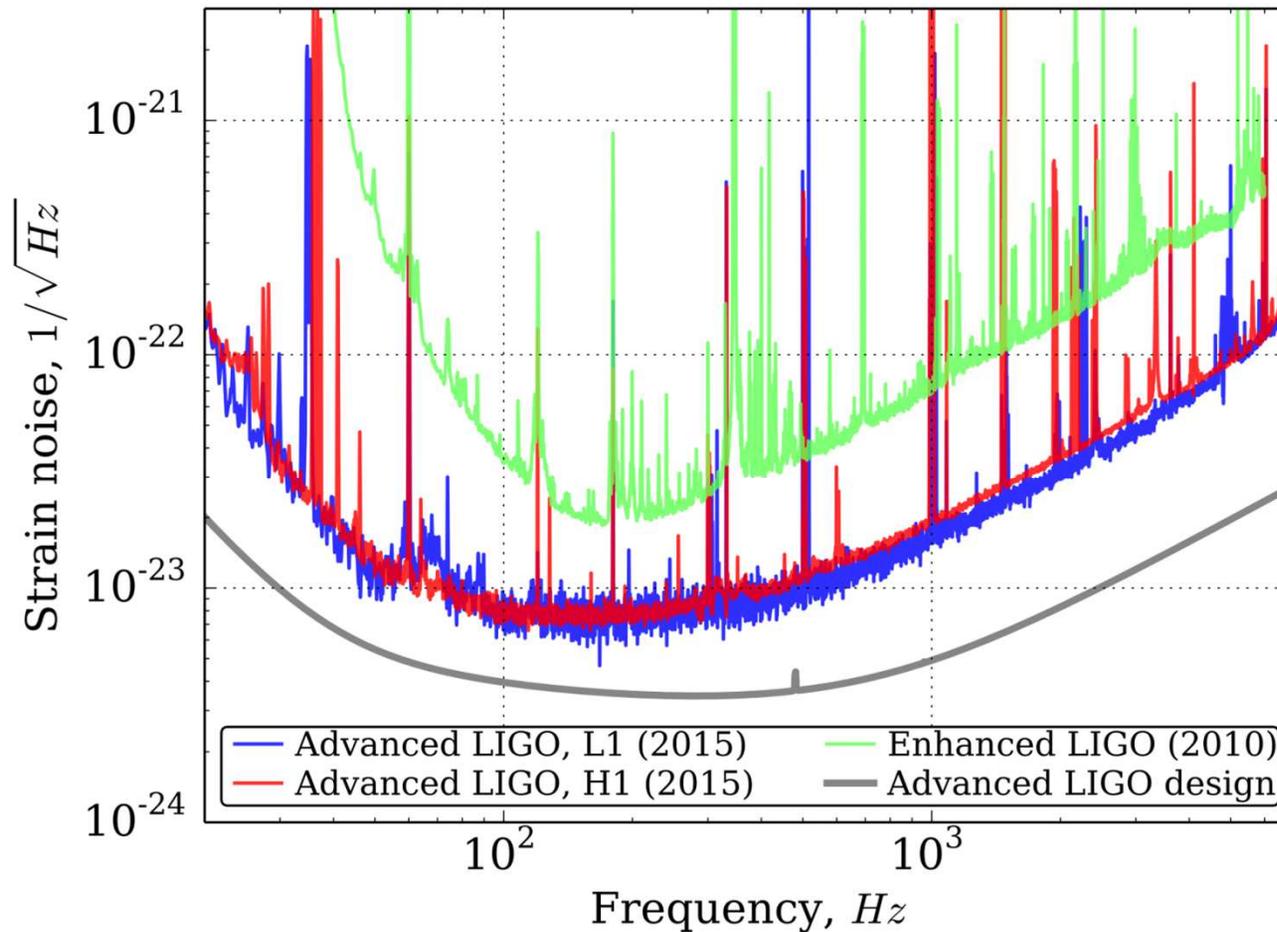
Act on the thicknesses →  $d_L, d_H$

Act on the materials →  $\eta_{L,H}$

total (H,L)-index material thickness, in units of local wavelength →  $d_L, d_H$

L,H material noisyness per unit thickness →  $\eta_{L,H}$

# LIGO Noise Floor Progress 2010-2015



[Martynov et al., PRD 93 (2016) 112004]

# The aLIGO Coatings

**Major breakthrough # 1 : the development of Ti doped Tantalum**  
[Harry et al, CQG 24 (2007) 405]

... Extensive trial and error testing (LMA, CSIRO) of alternative materials and dopants,  
500nm thick films

	Refraction index	Absorption (ppm)	Mechanical losses
Ta <sub>2</sub> O <sub>5</sub>	2.035	1.22	3·10 <sup>-4</sup>
Ta <sub>2</sub> O <sub>5</sub> : Co	2.11	5000	11·10 <sup>-4</sup>
Ta <sub>2</sub> O <sub>5</sub> : W	2.07	2.45	7.5·10 <sup>-4</sup>
Ta <sub>2</sub> O <sub>5</sub> : W+Ti	2.06	1.65	3.3·10 <sup>-4</sup>
→ Ta <sub>2</sub> O <sub>5</sub> : Ti	2.07	0.5	2.4·10 <sup>-4</sup>

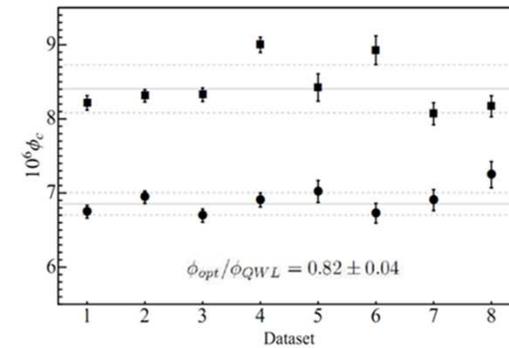
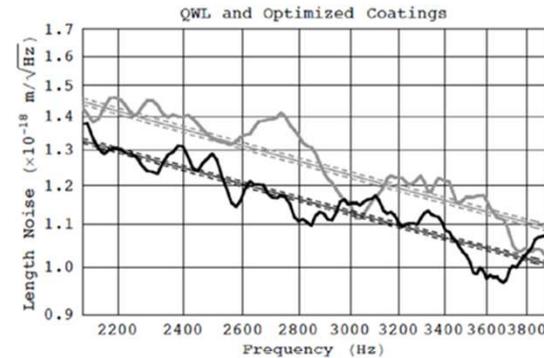
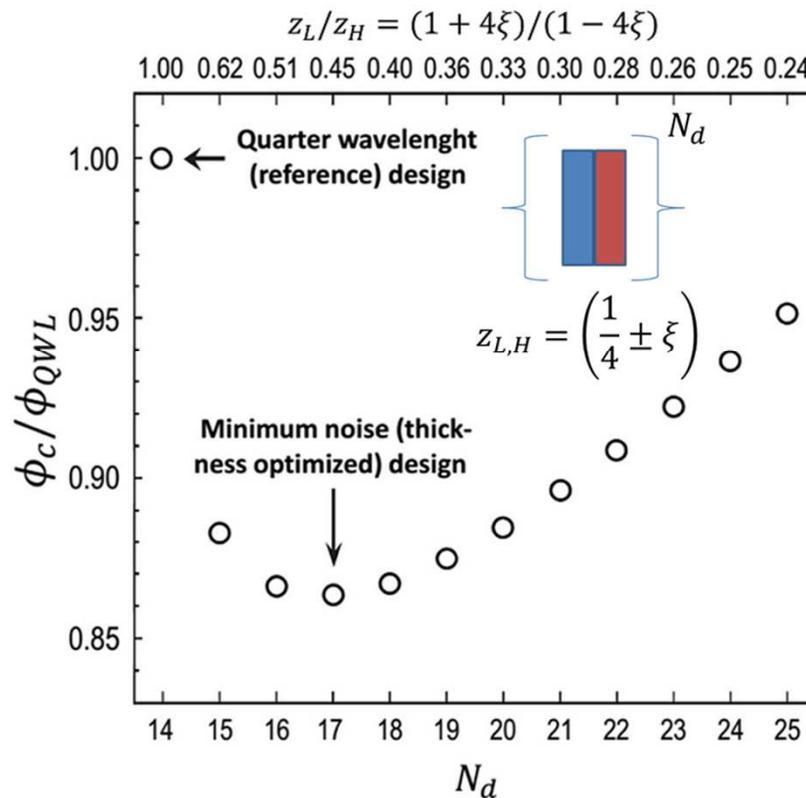
  

Coating	Refraction index	Absorption (ppm)	Mechanical losses
ZrO <sub>2</sub>	2.10	11	2.3·10 <sup>-4</sup>
ZrO <sub>2</sub> : Ti	2.15	37	6.8·10 <sup>-4</sup>
ZrO <sub>2</sub> : W	2.12	10	2.8·10 <sup>-4</sup>

[Flaminio et al., CQG 27 (2010) 84030] ...

# The aLIGO Coatings, contd.

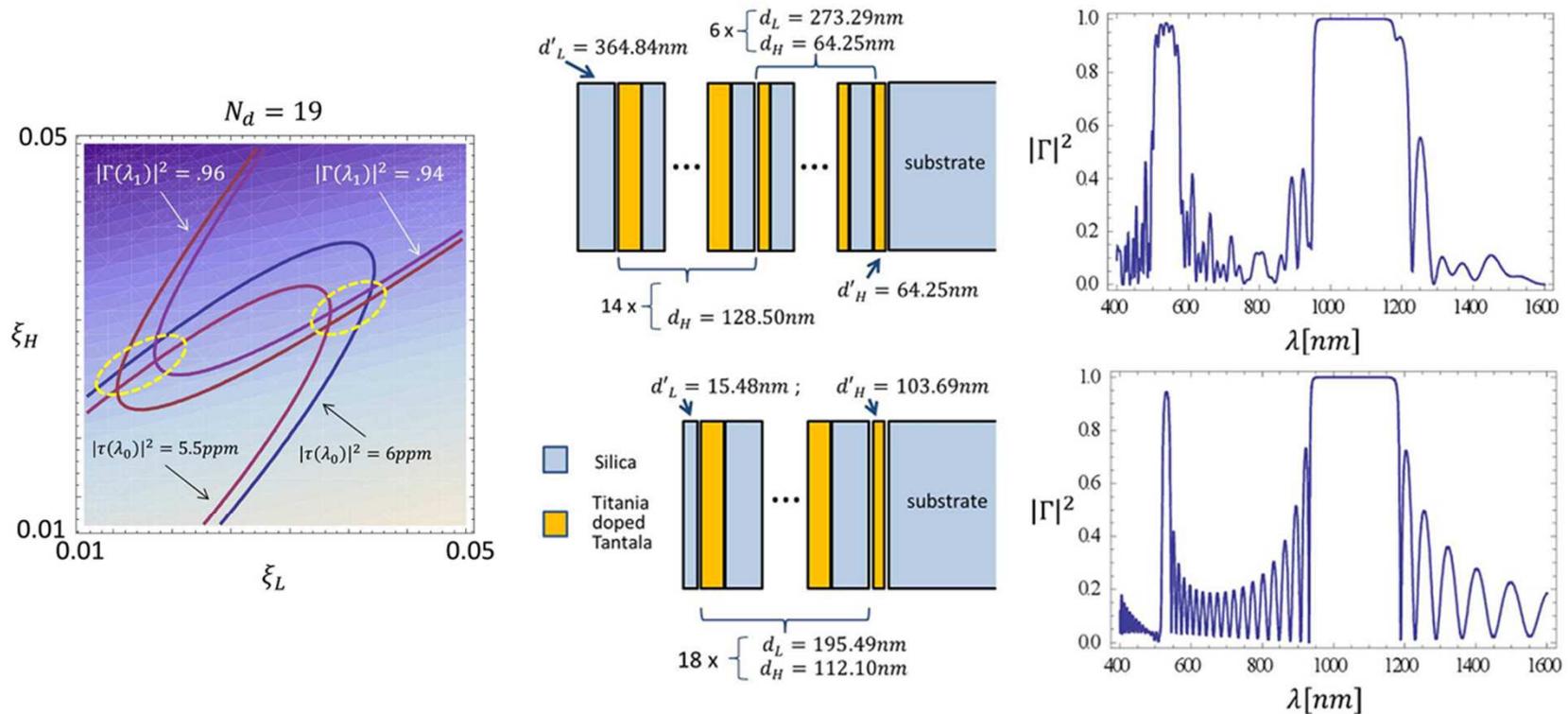
## Major breakthrough # 2 : coating thickness optimization



[Villar et al, PRD 81 (2010) 122001]

# The aLIGO Coatings, contd.

...used for the aLIGO dichroic mirrors [Principe et al., LIGO T080337]



[Principe, Optics Expr 23 (2015) 10938]

# Coating Science in “Milestone” Instrument Paper



→ The mirror coatings, a dielectric multilayer of silica and titania-doped tantala [30,31], were developed to provide the required high reflectivity while minimizing coating thermal noise [32–34]

(p. 131103-3)

[29] G. Harry, T. P. Bodiya, and R. DeSalvo, *Optical Coatings and Thermal Noise in Precision Measurement* (Cambridge University Press, Cambridge, England, 2012).

[30] G. M. Harry *et al.*, Titania-doped tantala/silica coatings for gravitational-wave detection, *Classical Quantum Gravity* **24**, 405 (2007).

[32] R. Flaminio, J. Franc, C. Michel, N. Morgado, L. Pinard, and B. Sassolas, A study of coating mechanical and optical losses in view of reducing mirror thermal noise in gravitational wave detectors, *Classical Quantum Gravity* **27**, 084030 (2010).

[33] J. Agresti, G. Castaldi, R. DeSalvo, V. Galdi, V. Pierro, and I. M. Pinto, Optimized multilayer dielectric mirror coatings for gravitational wave interferometers, *Proc. SPIE Int. Soc. Opt. Eng.* **6286**, 628608 (2006).

[34] A. E. Villar *et al.*, Measurement of thermal noise in multilayer coatings with optimized layer thickness, *Phys. Rev. D* **81**, 122001 (2010).

(p. 131103-6)

→ the Australian Research Council. The authors gratefully acknowledge the Italian Istituto Nazionale di Fisica Nucleare (INFN), the French Centre National de la Recherche

(p. 131103-5)

→\* I. M. Pinto,<sup>87</sup> – <sup>87</sup>University of Sannio at Benevento, I-82100 Benevento, Italy and INFN, Sezione di Napoli, I-80100 Napoli, Italy

# ... Large Part of that Work was “Made in Italy”!

## Optimized multilayer dielectric mirror coatings for gravitational wave interferometers

Juri Agresti<sup>a,b</sup>, Giuseppe Castaldi<sup>c</sup>, Riccardo DeSalvo<sup>a</sup>, Vincenzo Galdi<sup>c</sup>, Vincenzo Pierro<sup>c</sup>, and Innocenzo M. Pinto<sup>c</sup>

<sup>a</sup> LIGO Laboratory, California Institute of Technology, Pasadena, CA 91125, USA;

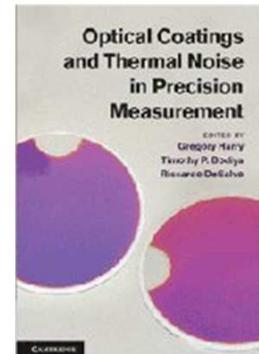
<sup>b</sup> Department of Physics, University of Pisa, I-56127, Pisa, Italy;

<sup>c</sup> Waves Group, Department of Engineering, University of Sannio, I-82100, Benevento, Italy

### ABSTRACT

The limit sensitivity of interferometric gravitational wave antennas is set by the thermal noise in the dielectric mirror coatings. These are currently made of alternating quarter-wavelength high/low index material layers with low mechanical losses. The quarter-wavelength design yields the maximum reflectivity for a fixed number of layers, but not the lowest noise for a prescribed reflectivity. This motivated our recent investigation of *optimal* thickness configurations, which guarantee the lowest thermal noise for a targeted reflectivity. This communication provides a compact overview of our results, involving *nonperiodic genetically-engineered* and *truncated periodically-layered* configurations. Possible implications for the advanced Laser Interferometer Gravitational wave Observatory (LIGO) are discussed.

Advances in Thin-Film Coatings for Optical Applications III, edited by Michael J. Ellison, Proc. of SPIE Vol. 6286, 628608, (2006) · 0277-786X/06/\$15 · doi: 10.1117/12.678977



ISBN: 9781107003385 (2012)

## 12 Reflectivity and thickness optimization

INNOCENZO M. PINTO, MARIA PRINCIPE, AND RICCARDO DESALVO

### 12.1 Introduction

This chapter is focused on design strategies for minimizing Brownian (see Chapter 4) and, more generally, thermal noises (see Chapters 3 and 9) in high-reflectivity optical coatings. It is organized as follows: in Section 12.2 we review the basic formulas needed to describe the optical properties of dielectric coatings (an *ab-initio* derivation of these formulas is included in the Appendix). Brownian noise formulas are the subject of Section 12.3. Section 12.4 presents the key ideas of coating thickness optimization. Thermo-optic noise issues are reviewed in Section 12.5, together with a discussion of pertinent minimization criteria. Section 12.6 contains a few comments on material characterization, and touches the important topic of glassy mixture modeling and optimization.

### 12.2 Coating formulas

In this section we summarize the basic coating formulas on which the subsequent analysis is based. A compact *ab-initio* derivation of these results is given in the Appendix.

Optical coatings are modeled as stacks of planar layers terminated on both sides by homogeneous halfspaces; the relevant geometry and notation is sketched in Figure 12.1. Layers are identified by an index  $i = 1, 2, \dots, N_L$ . It is understood that  $i = 0$  and  $i = N_L + 1$  correspond to the left halfspace and the substrate, respectively. It is convenient to introduce a local coordinate system  $(x, y, z)$  for each layer, so that the internal layers  $i = 1, 2, \dots, N_L$  correspond to  $-d_i \leq z \leq 0$ , the left halfspace is defined by  $-\infty < z \leq 0$ , and the substrate by  $0 \leq z, z_1 < \infty$ . Plane wave incidence from the leftmost halfspace is assumed.<sup>1</sup> An  $\exp(i2\pi ft)$  time dependence of the field is understood and omitted.

<sup>1</sup> This is the usual optical limit approximation. The general case of an incident Gaussian beam, and an optical limit, are discussed in Milton (1994).

Optical Coatings and Thermal Noise in Precision Measurement, eds. Gregory M. Harry, Timothy Boddy and Riccardo DeSalvo, Published by Cambridge University Press, © Cambridge University Press, 2012.

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PHYSICAL REVIEW D **81**, 122001 (2010)

## Measurement of thermal noise in multilayer coatings with optimized layer thickness

Akira E. Villar, Eric D. Black, Riccardo DeSalvo, and Kenneth G. Libbrecht

LIGO Laboratory, California Institute of Technology, Mail Code 264-33, Pasadena, California 91125, USA

Christophe Michel, Nazario Morgado, and Laurent Pinard

Laboratoire des Matériaux Avancés, Université Claude Bernard Lyon 1, CNRS/IN2P3, Villeurbanne, France

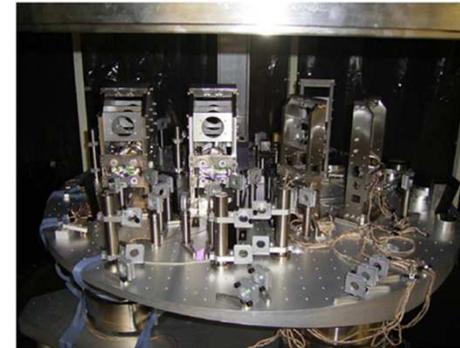
Innocenzo M. Pinto, Vincenzo Pierro, Vincenzo Galdi, Maria Principe, and Iliara Taurasi

Waves Group, University of Sannio at Benevento, Benevento, Italy, INFN and LSC

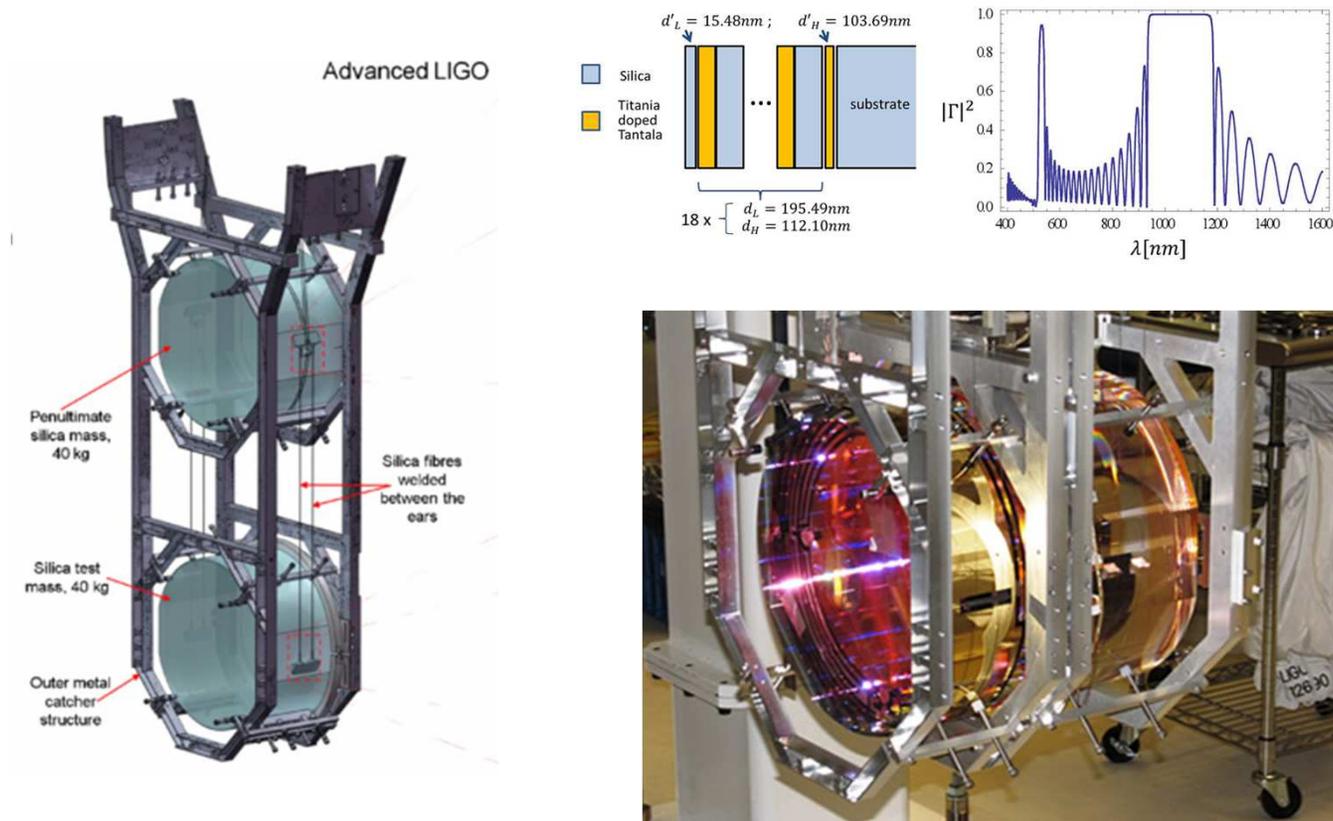
(Received 7 April 2010; published 3 June 2010)

A standard quarter-wavelength multilayer optical coating will produce the highest reflectivity for a given number of coating layers, but in general it will not yield the lowest thermal noise for a prescribed reflectivity. Coatings with the layer thicknesses optimized to minimize thermal noise could be useful in future generation interferometric gravitational wave detectors where coating thermal noise is expected to limit the sensitivity of the instrument. We present the results of direct measurements of the thermal noise of a standard quarter-wavelength coating and a low noise optimized coating. The measurements indicate a reduction in thermal noise in line with modeling predictions.

DOI: 10.1103/PhysRevD.81.122001



# The Advanced LIGO Mirrors



*Designed by the Usannio LSC Working Group, manufactured by LMA (Lyon, FR)*

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Ongoing Studies & New Ideas:

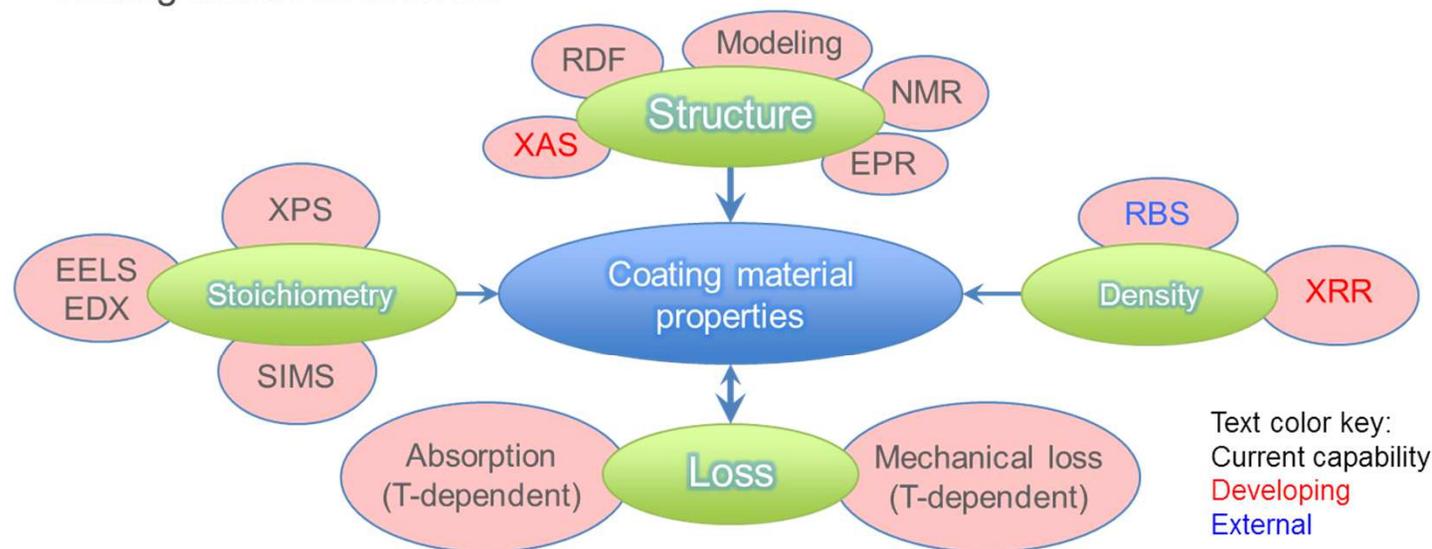
- Nanolayered Composites
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Conclusions

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# Atomic Level Investigations

- Experimental techniques that aim to link macroscopic material properties to the coating atomic structures:



- RDF – Reduced Density Function
- NMR – Nuclear Magnetic Resonance
- XAS – X-ray Absorption Spectroscopy
- XPS – X-ray Photoelectron Spectroscopy
- EPR – Electron Paramagnetic Resonance
- RBS – Rutherford Backscattering Spectrometry
- EELS – Electron Energy Loss Spectroscopy
- EDX – Energy Dispersive X-ray (Spectroscopy)
- XRR – X-ray Reflectometry
- SIMS – Secondary Ion Mass Spectrometry

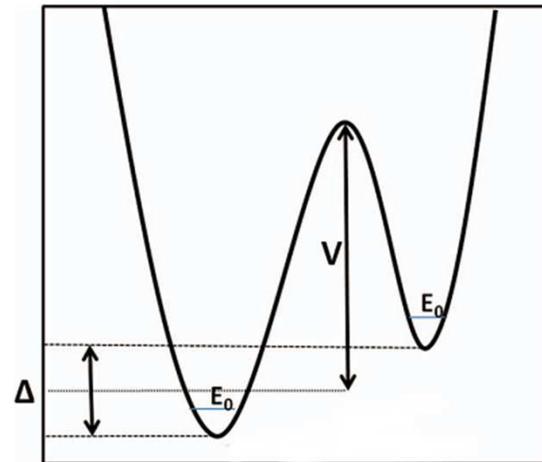
Working groups : Stanford, Glasgow

[Bassiri et al., LIGO-G100620]

# TLS Model

Acoustic (sound velocity & attenuation), dielectric (light velocity & attenuation) and thermal (specific heat & thermal conductivity) properties of amorphous solids display *generic features*, consistent with a model where local clusters of a few atoms/molecules may switch between two different configurations, as an effect of thermal or quantum fluctuations. Transitions produce dissipation, and hence noise.

The above two-level systems (TLS) are described (in suitable configuration coordinates) by double-well potentials, uniquely identified by the distributions of the barrier height  $V$ , unbalance  $\Delta$ , and switch time  $\tau$ .



[Gilroy & Phillips, Phil. Mag. B38 (1981) 735]

# TLS Model, contd.

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Mechanical losses (and other properties) can be derived from knowledge of those distributions via simple formulas [Pohl et al., *Rev. Mod. Phys.* 74 (2002) 991; Gilroy & Phillips, *Phil. Mag.* B38 (1981) 735].

➔ Both phonons and photons can drive TLS transitions. Measurements show that acoustic attenuation (mechanical loss) is reduced upon simultaneous RF exposure. [Laermans et al. *J. Phys. C: Solid State Phys.* 10 (1977) L161]. This is possibly interesting. (Brought to the attention of this Community by M. Abernathy)

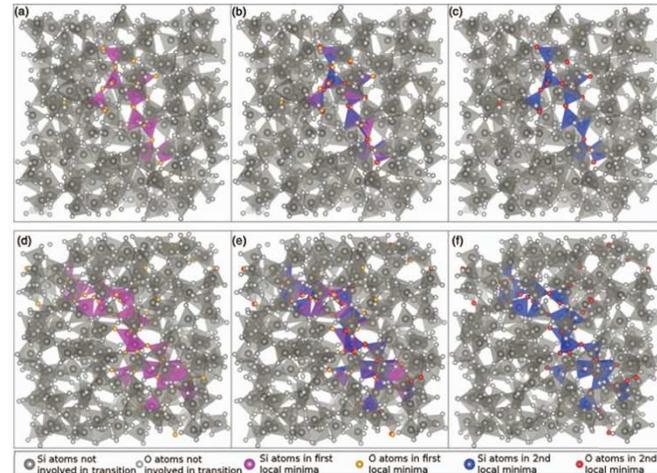
The TLS model is corroborated by brute force molecular modeling [Hamdan et al., *J. Chem. Phys.* 141 (2014) 054501; Trinastic et al., *Phys. Rev. B* 93 (2016) 014105],

# Molecular Dynamics

Investigates mechanical loss in amorphous oxides using classical MD software (e.g., DL-POLY) to calculate barrier height and asymmetry distributions, relaxation times, and deformation potentials.

Results match experimental trends  
Showing that that titania doping decreases the magnitude of the low-temperature loss peak in Tantalum.

May eventually help optimizing glassy oxide mixture formulations.



Silica - the top (panels (a)–(c)) involve 21 atoms; the bottom ones ((d)–(f)) 59. Atoms in gray are not involved in the transitions

**Working groups : UFL Gainesville**

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# Better Depositions

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- Films created by “hot” deposition ( $T \lesssim T_g$ ) featuring *negligible bulk mobility* but *large surface mobility* yield nearly **ideal glasses** with **almost no TLS** (thought of as due to energy landscape sampling by the depositing molecules).
- Such behavior is **observed in quite different materials**, e.g. *Indomethacin* [T. Perez et al., PNAS 111 (2014) 11275] and  *$\alpha$ -Silicon* [X. Liu et al., Phys. Rev. Lett. 113 (2014) 025503], and is **credited as generic** [Ediger, PNAS 111 (2014) 11232]



E-beam hot ( $T \sim 0.8 T_g$ ) deposited  $\alpha$ -Si films display TLS densities and elastic losses a factor 100 lower than conventional (LT deposited & HT annealed) films [X. Liu et al, *ibid.*]

# Better Depositions, contd.

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- ... a practical way [Kearns et al., J. Phys. Chem. B112 (2008) 4934] to check the (paradoxical/controversial) Kauzmann ansatz [Kauzmann, Chem. Rev. 43 (1948) 219]
  - ... yet to be proved for the glassy oxides of our interest ...
  - ... requires deposition tools enabling *high surface mobility* (high surface temperature) and *low deposition rates* [Singh et al., Nature Mat. 12 (2013) 139; ibid 13 (2014) 662; Lyubimov et al. J. Chem. Phys. 139 (2013) 144505]
  - **The required deposition temperature may be too high for the needed large(st) IBS systems**
  - **Enhanced mobility may boost crystallite formation → scattering**
-

# Smarter Doping

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Crystallization frustration following thermal annealing can be achieved also by doping.

Silica doping prevents Hafnia from crystallizing [Ushakov et al. Ph. Stat. Sol. B241 (2004) 2800]; Zirconia doping prevents Tantalum from crystallizing [Penn LIGO-G1301031]; Silica prevents Zirconia from crystallizing [Penn, LIGO-G1300306], etc.

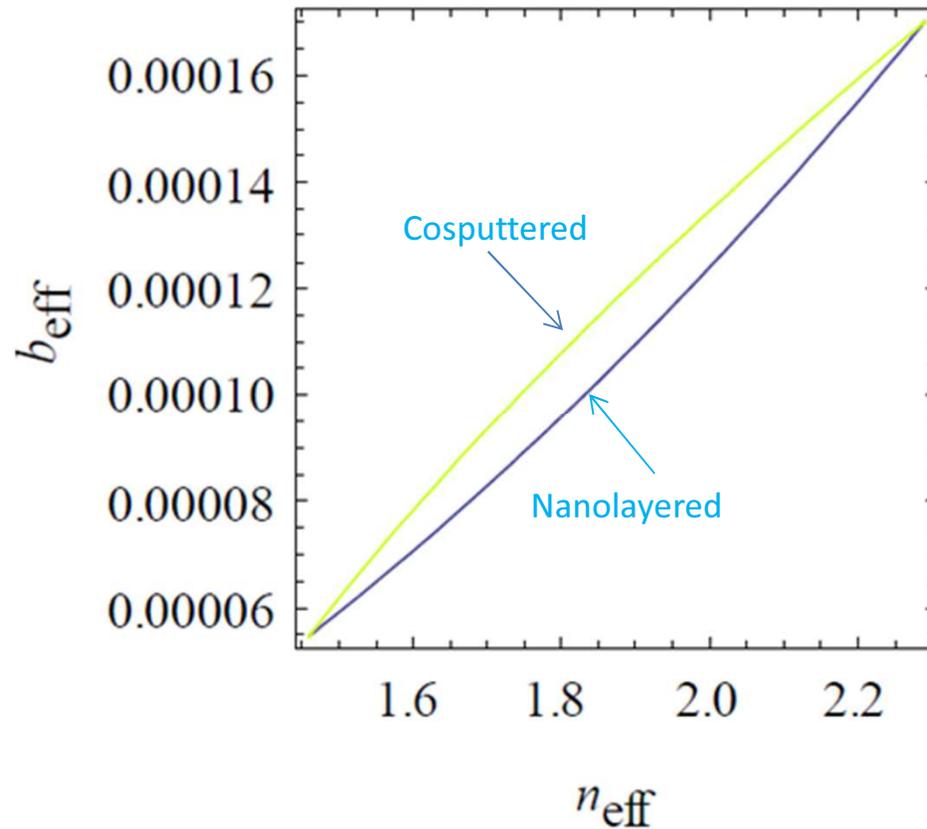
Doping may have different effects: Titania affects strongly Oxygen-Tantalum coordination, reducing mechanical losses in Ta<sub>2</sub>O<sub>5</sub>; Hydrogen doping reduces mechanical losses in  $\alpha$ -Si, etc.

One may use *different dopants together*, to obtain different effects...  
... or use *(nano)-stratified mixtures*

# Nanolayered vs Cosputtered

SiO<sub>2</sub>/TiO<sub>2</sub> Composites

[I. Pinto, LIGO-G1100586]



**Nanolayered SiO<sub>2</sub>/TiO<sub>2</sub> composites are *less noisy*, compared to co-sputtered SiO<sub>2</sub>/TiO<sub>2</sub> composites having the same refraction index**

# University-Scale Coating Facilities

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... involved in GW detector collaborations (**as of Jan 2017**)

- **UCB**, Berkeley CA, USA (PI Frances Hellman)  
*EB, RF-MS, PDC-R-MS*
- **CSU**, Fort Collins CO, USA (PI Carmen Menoni)  
*(D)IBS*
- **NAOJ/ATC**, Tokyo, JP (PI Waseda Kouichi)  
*IBS*
- **NTHU**, Taipei, TW (PI Shih Chao)  
*IBS, CVD*
- **UWS**, Paisley, UK (PI Stuart Reed)  
*PA-EB, MA-RS, PE-CVD, IA-RFS*
- **USANNIO**, Benevento, IT (PI Maria Principe)  
*PA(D)EB*

# University-Scale Coating Facilities, contd.

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## Abbreviations:

- *EB = Electron Beam Gun Evaporator*
- *RF-MS =Radio Frequency Microwave Sputtering*
- *PDC-R-MS =Pulsed DC Reactive Magnetron Sputtering*
- *(D)IBS = (Dual) Ion Beam Sputtering*
- *PA-EB = Plasma Assisted EB*
- *MA-RS = Microwave assisted Reactive Sputtering,*
- *PE-CVD =Plasma Enhanced Chemical Vapor Deposition*
- *IA-RFS – Ion Assisted Radio Frequency Sputtering*
- *PA(D)EB = Plasma Assisted (Dual) EB*

# The USannio Coating Facility

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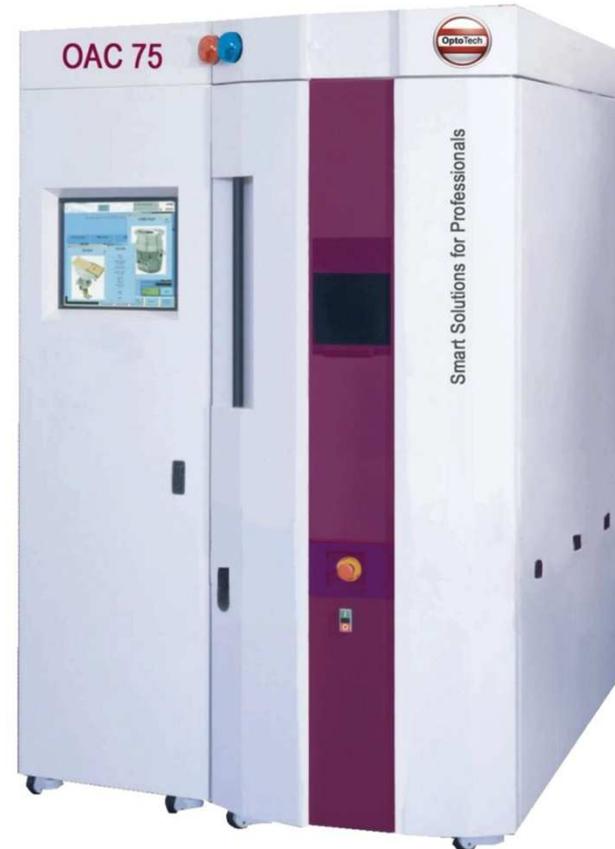
## Custom version of Optotech OAC-75

- Plasma assisted deposition
- High quality /density of layers
- Dual eb-gun
- Multimaterial
- Fully programmable
- Substrate heating
- R&D configuration
- IBS as possible add-on

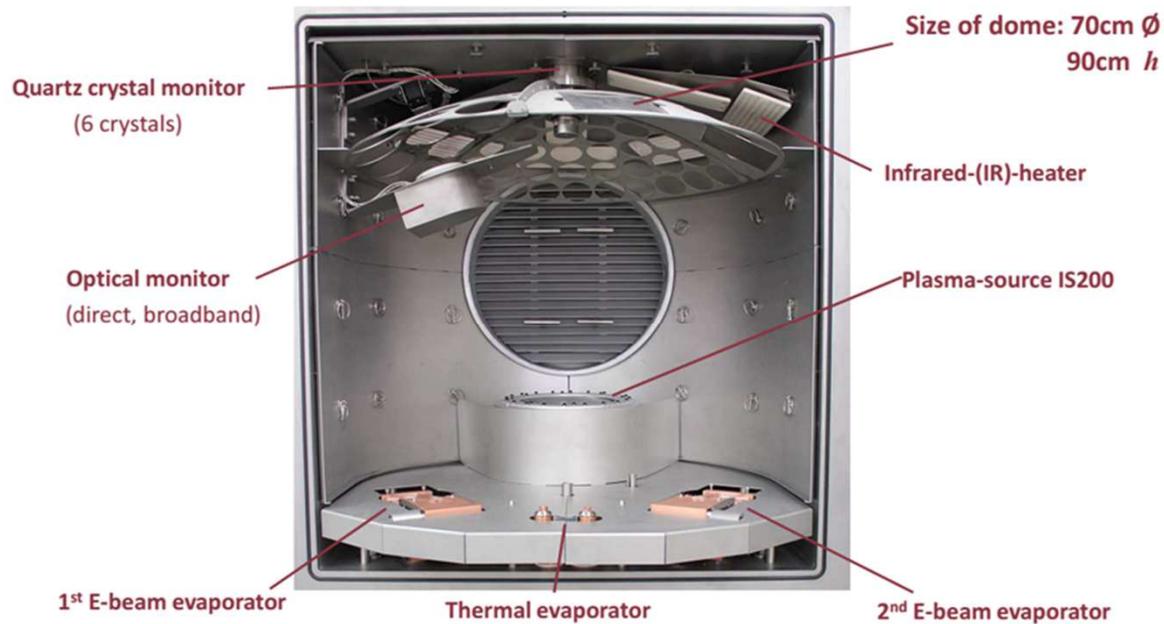
Cost ~ 0.6 MEUR

Funding by Regione Campania (FESR,  
University research empowering program)

**Should start operation in spring 2017**



# The USannio Coating Facility, contd.



## [Ferrotec EVM-8 eb-gun systems]

- 2 eb-guns
- Multiple (6) pocket configuration
- Evaporation of all kind of oxides (and metals)
- Co-evaporation of different optical materials possible
- Freely adjustable HV from 6 to 8 kV (layer-to-layer)
- Sweep parameters and sweep pattern easy preset
- Variable pocket rotation speed (single pocket)

## (COPRA® IS200 plasma source)

- Built-in source w. flexible position & changeable inclination
- Powered @ 13.56 MHz, max. power 1500 W
- Large beam extraction Ø 110 mm for uniform distribution
- Ion energy 50 to 180 eV
- Ion current density up to 0.5 mA/cm<sup>2</sup>
- Pressure range 1E-4 to 1E-3 mbar
- Operation with pure oxygen possible
- Highest n-values for stress free films

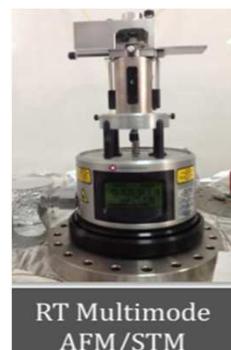
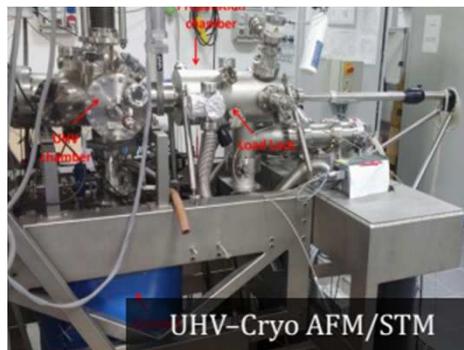
Built in GUI-based MacroTech control unit enables fully automated process control

# The USannio Coating Facility, contd.

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## UniSa Nanotechnology Lab Facilities (F. Bobba, C. Di Giorgio)

- X-Ray Diffractometer X'PERT MRD-PRO (Philips)
- UHV-variable temperature AFM/STM (Omicron)
- Room temperature AFM/AFS MM5 (Bruker Nanowizard3 JPK)
- SEM EVO50 (Zeiss) ; FeSEM Sigma GEMINI (Zeiss) ; TEM TMG2 (Fei)



# Outlook

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Why Coating R&D

Where are we now : the aLIGO mirrors

How can we progress:



- Improving Modeling
- Improving Processes
- Improving Characterization

Ongoing Studies & New Ideas:

- Nanolayered Composites
- Silicon Nitrides
- Crystalline Coatings
- M-ary Coatings
- Metamaterial Coatings

Conclusions

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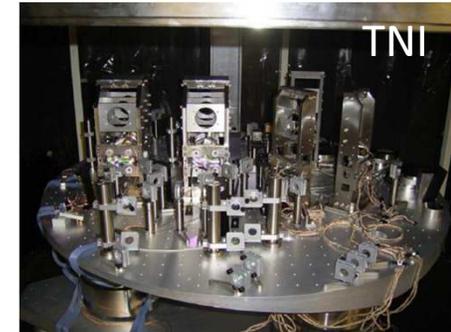
# Direct TN Measurement : TNI etc.

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## Original TNI

[Numata et al., Phys. Rev. Lett. 91 (2003) 260602]

[Black et al., Phys. Lett. A 328 (2004) 1]



## Available facilities

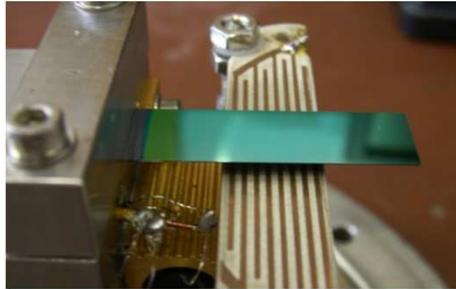
- LMA (QDI) [Paolino et al., Rev. Sci. Instrum. 84, 2013]
- Caltech (TNI) [Chalermsongsak et al., Metrologia 52 (2015) 17]
- MIT (CTN) [Gras et al., Phys. Rev. D95, 022001 (2017)]

## Other facilities (under development)

- AEI (10m facility), [Wohler et al. LIGO-P1600260]
- UFL, (Cryo-Thor) [Mueller et al., LIGO-G1600076]



# Mechanical Loss from Ringdown : the Cantilever



$$Q_c^{-1} = Q^{-1} + \frac{\langle W_s \rangle}{\langle W_c \rangle} (Q^{-1} - Q_s^{-1})$$

$$\frac{\langle W_c \rangle}{\langle W_s \rangle} = \frac{\int_{h_s}^{h_s+h_c} (z-z_0)^2 \frac{E(z)}{(1-\sigma(z)^2)} dz}{\int_0^{h_s} (z-z_0)^2 \frac{E(z)}{(1-\sigma(z)^2)} dz} \approx \frac{E_s h_s}{3E_c h_c}$$

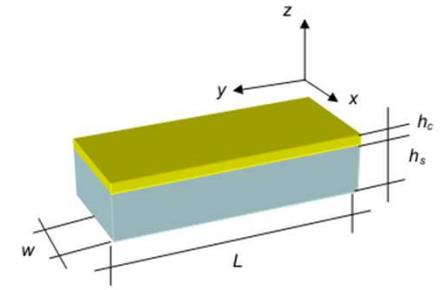


Fig. 1 – Problem's geometry and notation

LIGO – T060173

**LIGO**

LIGO Laboratory / LIGO Scientific Collaboration

LIGO-T060173-00-R Date August 3 2006

**Measuring Coating Mechanical Quality Factors in a Layered Cantilever Geometry: a Fully Analytic Model**

Vincenzo Pinto, Innocenzo M. Pinto  
TIRG, University of Salerno at Benevento, ITA

Distribution of this document:  
LIGO Science Collaboration

This is an internal working note  
of the LIGO Project.

**Reduction of tantala mechanical losses in Ta<sub>2</sub>O<sub>5</sub>/SiO<sub>2</sub> coatings for the next generation of VIRGO and LIGO interferometric gravitational waves detectors**

Christophe Comtet <sup>a,\*</sup>, Danièle Forest <sup>a</sup>, Patrick Ganau <sup>a</sup>, Gregory M Harry <sup>b</sup>, Jean Marie Mackowski <sup>a</sup>, Christophe Michel <sup>a</sup>, Jean Luc Montorio <sup>a</sup>, Nazario Morgado <sup>a</sup>, Vincenzo Piero <sup>c</sup>, Laurent Pinard <sup>a</sup>, Innocenzo Pinto <sup>c</sup> and Alban Remillieux <sup>a</sup>

<sup>a</sup> Laboratoire des Matériaux avancés, CNRS, France  
<sup>b</sup> LIGO Laboratory, Massachusetts Institute of Technology, NW17-161, Cambridge, MA 01239, USA  
<sup>c</sup> Waves Group, Department of Engineering, University of Salerno, I-84106, Benevento, Italy

**Abstract**

Mirror thermal noise in Ta<sub>2</sub>O<sub>5</sub>/SiO<sub>2</sub> coatings is predicted to be the limiting noise in the 50-300 Hz frequency range in the interferometric gravitational wave detectors. Ta<sub>2</sub>O<sub>5</sub> losses were dominating compared to the SiO<sub>2</sub> losses. We developed a model to calculate multilayer mechanical losses and we are working for low mechanical losses Ta<sub>2</sub>O<sub>5</sub>/SiO<sub>2</sub> coatings.

**Keywords:** Gravitational waves; thermal noise; mechanical losses

[in 42th Rencontres de Moriond :  
Gravitational Waves and Experimental Gravity, 2007]

# Mechanical Loss from Ringdown : GeNS

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The Gentle nodal Suspension (GeNS) is to date the most reliable mechanical loss estimation setup based on ringdown measurement.

Several improvements compared to clamped cantilever systems;

Designed to be exempt from re-clamping issues, yields nicely repeatable results.

Multimode operation should allow measurement of bulk/shear loss angles (TBD).



## Available facilities:

- LMA (G. Cagnoli)
- Rome-TV (E. Cesarini)
- Caltech (G. Vajente)

[Cesarini et al., Rev. Sci. Instrum. 80 (2009) 053904.]

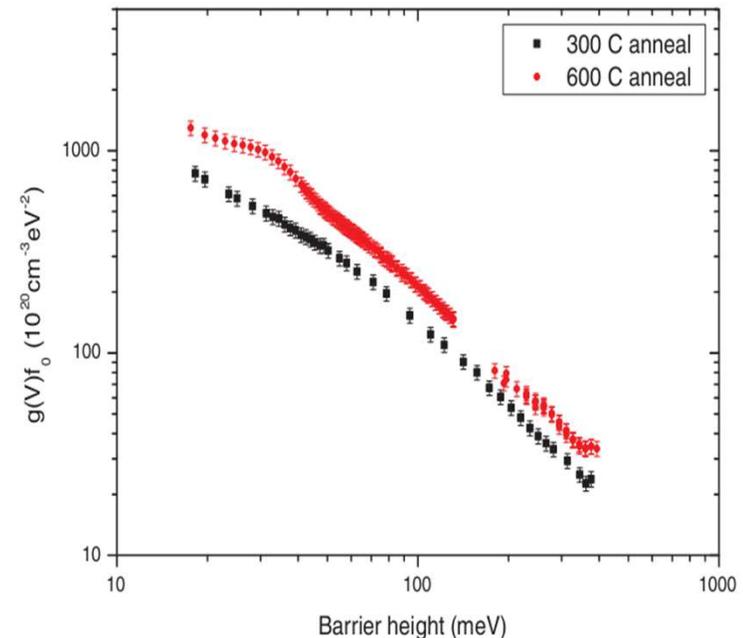
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# Cryogenic Loss Measurements

- Are needed for downselection of coating materials to be used in 3<sup>rd</sup> generation (cryogenic) GW detectors;
- Can be used to retrieve the activation energy and relaxation time distributions of a TLS model, **from the frequency dependence of the loss peak temperature** by plotting  $\log[f]$  vs  $T$ , so as to obtain  $(E_a, \tau)$ , in view of

$$2\pi f\tau \exp[E_a/kT] = 1$$

- Help understanding how deposition & annealing affect losses.



**Available facilities : several, e.g.  
Glasgow, LMA, NTHU ,  
Perugia, Rome, Stanford, etc.**

[Martin et al., CQG 27 (2010) 225020]

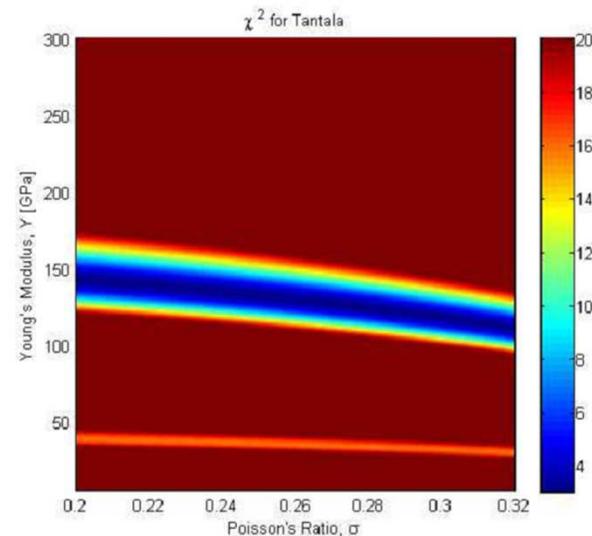
# Measuring Elastic Moduli ( $Y, \sigma$ )

Several techniques proposed : acoustic (ERAU), nano-indentation (Glasgow) , resonance-shift (USannio), partly complementing.

Working facilities at

- ERAU [A. Gretarsson (a)]
- Glasgow [I. Martin (n)]
- Caltech [M. Abernathy (n)]
- LMA [G. Cagnoli (n)]

Not only an ingredient of the coat-TN formula, but also needed to compute the *dilution factors* relating material loss angles to measured ringdown damping times.



[Rhoades et al., LIGO-T1500147]

[Abernathy et al., Appl. 53 (2014) 3196]

# Direct (TNI) vs Ringdown

Material	Layer thickness (nm)	$\phi$ ( $\times 10^{-4}$ )	Setup/ref
SiO <sub>2</sub>	90.8–272.3	$0.5 \pm 0.3$	Suspended disks [12]
	181.5–250.984	$0.51 \pm 0.07$	TNI
	500	$0.5 \pm 0.018$	Clamped cantilevers [27]
	500	$0.46 \pm 0.01$	Clamped cantilevers [28]
	3,070	$0.6 \pm 0.03$	Quad. Phase Diff. IFO [29]
Ta <sub>2</sub> O <sub>5</sub>	65.36–196.07	$4.4 \pm 0.2$	Suspended disks [12]
	80.688–130.713	$4.72 \pm 0.14$	TNI
	133	$3.3 \pm 0.9$	GeNS [30]
	500	$3.02 \pm 0.11$	Clamped cantilevers [27]
	3,130	$4.7 \pm 0.2$	Quad. Phase Diff. IFO [29]
TiO <sub>2</sub> :Ta <sub>2</sub> O <sub>5</sub>	112.10–128.8	$3.66 \pm 0.26$	TNI
	500	$2.4 \pm 0.4$	Clamped cantilevers [28]

## References

- [12] S. D. Penn et al., CQG 20 (2003) 2917  
 [27] Ch. Comtet et al., Proc. 42th Renc. Moriond (2007)  
<http://hal.in2p3.fr/docs/00/17/75/78/PDF/Conf3.pdf>  
 [28] R. Flaminio et al., Proc. GWADW 2013 (Elba)  
<https://agenda.infn.it/getFile.py/access?contribId=105&sessionId=26&resId=0&materialId=slides&confId=5484>  
 [29] M. Granata et al., Proc. GWADW 2014 (Takayama)  
[http://www.gravity.ircs.titech.ac.jp/GWADW2014/slide/Massimo\\_Granata.pdf](http://www.gravity.ircs.titech.ac.jp/GWADW2014/slide/Massimo_Granata.pdf)  
 [30] E. Cesarini et al., J. Non-Cryst. Solids 357 (2011) 2005  
 [41] R. Flaminio et al., Proc. 9th Amaldi Conference,  
[http://www.amaldi9.org/abstracts/420/Flaminio\\_Amaldi\\_2011\\_July11.pdf](http://www.amaldi9.org/abstracts/420/Flaminio_Amaldi_2011_July11.pdf)

**Direct (TNI-derived) loss angle estimates [Principe et al, Phys Rev. D-91 (2015) 022005] are in good agreement with available (LMA) quad-phase differential interferometry results (Silica and Plain Tantal).**

[Principe et al., PRD 91 (2015) 022005]

# More Loss Measurement Puzzles

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## Puzzle # 1 (multilayers)

Use (measured) loss angle of multilayer, and (measured) loss angle of single low (resp. high) index material to estimate loss angle of high (resp. low) index material. Results are inconsistent :

$$\begin{array}{l} \phi_{H^*} = (2.4 \pm 0.2) \cdot 10^{-4} \\ \phi_L = (0.5 \pm 0.1) \cdot 10^{-4} \end{array} \quad \begin{array}{l} \Longrightarrow \\ \Longrightarrow \end{array} \quad \begin{array}{l} \phi_L = (1.3 \pm 0.4) \cdot 10^{-4} \\ \phi_{H^*} = (4.2 \pm 0.2) \cdot 10^{-4} \end{array}$$

## Puzzle # 2 (multilayers)

**Double-face vs single face coating :**

- 1) suppresses (post annealing) substrate bending.
- 2) total loss should be doubled, i.e.,  $Q_2 = Q_1 / 2$

**Measurements :** confirm this for single-layer films;

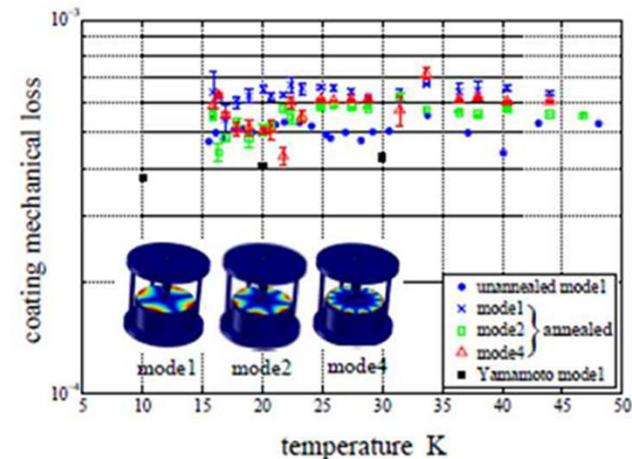
instead, for multi-layers, one gets  $Q_2 > Q_1 / 2$ .

**does bending suppression alleviate interface friction ?**

# More Loss Measurement Puzzles

Mechanical loss measurements on multi-layer Titania-doped-Tantala/Silica coatings on Silicon (annealed at 400 C~ 600 C) show a cryo-peak at  $\sim 30\text{K}$  [Granata et al., Opt. Lett. 38, 5268 (2013)].

Mechanical loss measurements on multi-layer Tantala/Silica coatings on Sapphire do *not* show such peak, yielding almost temperature-independent losses [Yamamoto et al., PRD-74 022002 (2006); Hirose et al., LIGO-P1400107].



**Reasons behind these discrepancies yet to be understood .**

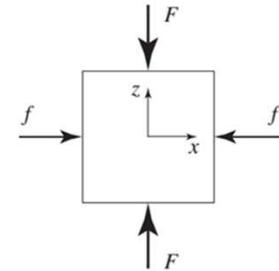
# Issues with $\phi_{\parallel}$ , $\phi_{\perp}$

- 1) “Traditional” definition of coating loss angle [Harry et al., CQG 29 (2002) 897]

$$\frac{\phi_c}{d} = \left( \frac{\delta U_{\parallel}}{U} \right) \phi_{\parallel} + \left( \frac{\delta U_{\perp}}{U} \right) \phi_{\perp}, \text{ where}$$

$$\delta U_{\parallel} = \int_s \frac{1}{2} (S_{xx} T_{xx} + S_{yy} T_{yy}) dx dy$$

$$\delta U_{\perp} = \int_s \frac{1}{2} S_{zz} T_{zz} dx dy$$



is ill defined, as the “Energies”  $\delta U_{\parallel}$ ,  $\delta U_{\perp}$  can be negative in some cases (e.g. symmetrically squeezed cube).

[Hong, PhD Thesis., Caltech 2013]

- 2) “Traditional” definition of  $\phi_{\parallel}$ ,  $\phi_{\perp}$  [Harry et al., CQG 29 (2002) 897]

$$\phi_{\perp} = Y_{\perp} \left( \frac{Y_1^{-1} \phi_1 d_1 + Y_2^{-1} \phi_2 d_2}{d_1 + d_2} \right), \quad \phi_{\parallel} = Y_{\parallel}^{-1} \left( \frac{Y_1 \phi_1 d_1 + Y_2 \phi_2 d_2}{d_1 + d_2} \right)$$

Holds, strictly, only for  $\sigma_1 = \sigma_2 = 0$  (which implies  $\phi_B = \phi_S$ ).

[Somiya, LIGO T0900033v1]

# ...Use Bulk & Shear Loss Angles

Write elastic energy in terms of bulk and shear deformations/stresses

$$U = \frac{1}{2} K \Theta^2 + \mu \Sigma_{ij} \Sigma_{ij}$$

↗ ↖  
 bulk / shear energies

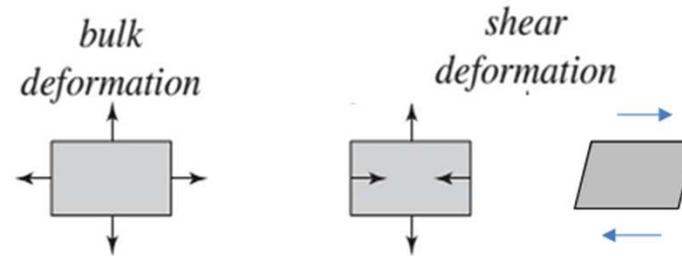
where  $\left\{ \begin{array}{l} \Theta = S_{ii}, S = \text{stress tensor} \\ \Sigma = \frac{1}{2}(S_{ij} + S_{ji}) - \frac{1}{3}g_{ij}S_{kk} \end{array} \right.$

Express coating loss angle in terms of bulk/shear loss angles

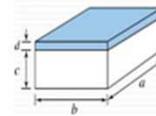
$$\frac{\phi_c}{d} = \left( \frac{\delta U_B}{U} \right) \phi_B + \left( \frac{\delta U_S}{U} \right) \phi_S$$

↗ ↖  
 bulk/shear dilution factors

Calculate dilution factors using FEA.  
 Requires accurate knowledge of coating (bulk) Young and Poisson moduli.



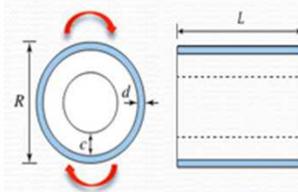
## 1) Bending (Transverse) Modes of Coated Thin Rectangular Plate



$$\phi = \frac{d Y_c (1 - \sigma_s^2)}{c Y_s (1 - \sigma_c)^2} \left[ \phi_B (1 - 2\sigma_c) + 2\phi_s \frac{1 - \sigma_c + \sigma_c^2}{1 + \sigma_c} \right] + \phi_{sub}$$

## 2) Torsional Modes of Coated Thin Hollow Cylinder

[L. H. Donnell, NACA Rept 479, (1933)]



$$\phi = \phi_{sub} + \frac{d Y_c (1 + \sigma_s)}{c Y_s (1 + \sigma_c)} \phi_s$$

[T. Hong, PhD Thesis, Caltech, 2013]

[Harry, LIGO-G1500109]

# Bulk & Shear Loss Angle Measurement

... from measured ringdown of several butterfly (b) and drumhead (d) modes via

$$\begin{matrix} \text{measured} & \text{dil. factor matrix (FEA, known)} & \text{sought} \\ \begin{pmatrix} \phi_b \\ \phi_d \\ \dots \end{pmatrix} & = \begin{pmatrix} R_{bulk-b} & R_{shear-b} \\ R_{bulk-d} & R_{dhear-d} \\ \dots & \dots \end{pmatrix} & \begin{pmatrix} \phi_B \\ \phi_S \\ \dots \end{pmatrix} \end{matrix}$$

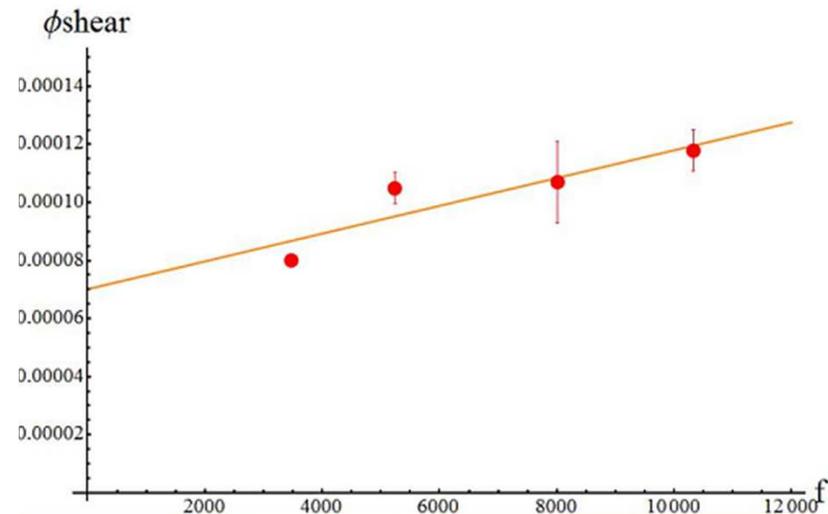
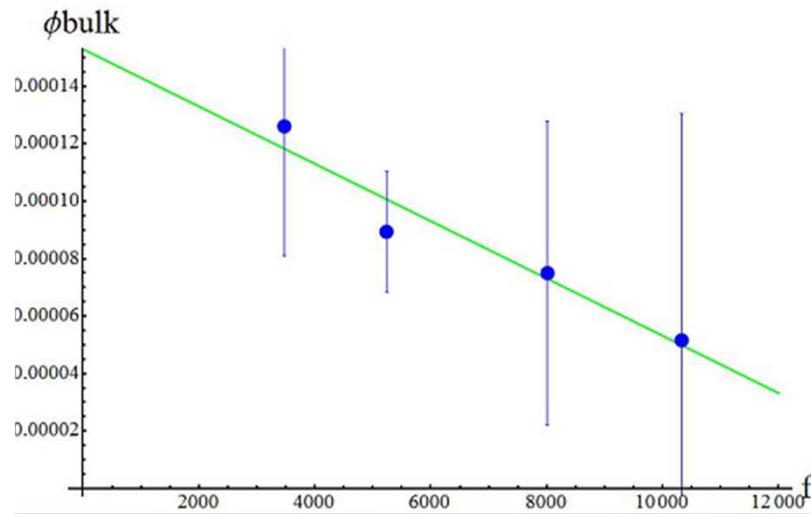
[Abernathy, LIGO-G1300163  
 Harry et al., LIGO-G1400803  
 Harry et al., LIGO-G1400961  
 Abernathy, LIGO-G1500109]

Mode	Frequency	Q	$\delta Q$	$R_{shear}$	$R_{bulk}$
BF	2773 Hz	$1.14 \times 10^6$	$2.5 \times 10^3$	$9.93 \times 10^{-3}$	$6.58 \times 10^{-4}$
DH	4178 Hz	$8.70 \times 10^5$	$2.6 \times 10^4$	$6.85 \times 10^{-3}$	$4.79 \times 10^{-3}$
Hex	6307 Hz	$9.32 \times 10^5$	$3.2 \times 10^4$	$9.37 \times 10^{-3}$	$9.65 \times 10^{-4}$
DDH	9707 Hz	$9.16 \times 10^5$	$3.8 \times 10^3$	$7.68 \times 10^{-3}$	$3.62 \times 10^{-3}$
Oct	10943 Hz	$8.87 \times 10^5$	$1.6 \times 10^4$	$9.05 \times 10^{-3}$	$1.18 \times 10^{-3}$

# $\phi_B, \phi_S$ Measured

[ Harry et al., LIGO-G1400961]

(LMA Titania doped Tantala)



Fits:

$$\phi_B = 1.5 \cdot 10^{-4} - 1.0 \cdot 10^{-8} f$$
$$\phi_S = 7.0 \cdot 10^{-5} - 4.8 \cdot 10^{-9} f$$



$$\phi_B / \phi_S \approx 2$$

# Elastic Moduli – Conversion Table

Linear homogeneous isotropic elastic response can be described in terms of *any pair* of (complex) elastic moduli chosen among  $E$  (Young),  $\nu$  (Poisson),  $K$  (bulk),  $G$  (shear),  $M$  (longitudinal), and  $\lambda$  (1<sup>st</sup> Lamé’).

Good sense recipe:  
use (hopefully more accurate) measured complex Bulk & Shear moduli in *usual* (Harry’s) coating noise formula based on  $Y$  (aka,  $E$ ) and  $\sigma$  (aka,  $\nu$ ) ...

Purple (resp., red) arrows show how to get  $(E, \nu)$  from  $(K, G)$  (resp.,  $(K, G)$  from  $(E, \nu)$ ).

	 $K =$	 $E =$	$\lambda =$	 $G =$	 $\nu =$	$M =$
$(K, E)$	$K$	$E$	$\frac{3K(3K-E)}{9K-E}$	$\frac{3KE}{9K-E}$	$\frac{3K-E}{6K}$	$\frac{3K(3K+E)}{9K-E}$
$(K, \lambda)$	$K$	$\frac{9K(K-\lambda)}{3K-\lambda}$	$\lambda$	$\frac{3(K-\lambda)}{2}$	$\frac{\lambda}{3K-\lambda}$	$3K - 2\lambda$
$(K, G)$	$K$	$\frac{9KG}{3K+G}$	$K - \frac{2G}{3}$	$G$	$\frac{3K-2G}{2(3K+G)}$	$K + \frac{4G}{3}$
$(K, \nu)$	$K$	$3K(1-2\nu)$	$\frac{3K\nu}{1+\nu}$	$\frac{3K(1-2\nu)}{2(1+\nu)}$	$\nu$	$\frac{3K(1-\nu)}{1+\nu}$
$(K, M)$	$K$	$\frac{9K(M-K)}{3K+M}$	$\frac{3K-M}{2}$	$\frac{3(M-K)}{4}$	$\frac{3K-M}{3K+M}$	$M$
$(E, \lambda)$	$\frac{E+3\lambda+R}{6}$	$E$	$\lambda$	$\frac{E-3\lambda+R}{4}$	$\frac{2\lambda}{E+\lambda+R}$	$\frac{E-\lambda+R}{2}$
$(E, G)$	$\frac{EG}{3(3G-E)}$	$E$	$\frac{G(E-2G)}{3G-E}$	$G$	$\frac{E}{2G} - 1$	$\frac{G(4G-E)}{3G-E}$
$(E, \nu)$	$\frac{E}{3(1-2\nu)}$	$E$	$\frac{E\nu}{(1+\nu)(1-2\nu)}$	$\frac{E}{2(1+\nu)}$	$\nu$	$\frac{E(1-\nu)}{(1+\nu)(1-2\nu)}$
$(E, M)$	$\frac{3M-E+S}{6}$	$E$	$\frac{M-E+S}{4}$	$\frac{3M+E-S}{8}$	$\frac{E-M+S}{4M}$	$M$
$(\lambda, G)$	$\lambda + \frac{2G}{3}$	$\frac{G(3\lambda+2G)}{\lambda+G}$	$\lambda$	$G$	$\frac{\lambda}{2(\lambda+G)}$	$\lambda + 2G$
$(\lambda, \nu)$	$\frac{\lambda(1+\nu)}{3\nu}$	$\frac{\lambda(1+\nu)(1-2\nu)}{\nu}$	$\lambda$	$\frac{\lambda(1-2\nu)}{2\nu}$	$\nu$	$\frac{\lambda(1-\nu)}{\nu}$
$(\lambda, M)$	$\frac{M+2\lambda}{3}$	$\frac{(M-\lambda)(M+2\lambda)}{M+\lambda}$	$\lambda$	$\frac{M-\lambda}{2}$	$\frac{\lambda}{M+\lambda}$	$M$
$(G, \nu)$	$\frac{2G(1+\nu)}{3(1-2\nu)}$	$2G(1+\nu)$	$\frac{2G\nu}{1-2\nu}$	$G$	$\nu$	$\frac{2G(1-\nu)}{1-2\nu}$
$(G, M)$	$M - \frac{4G}{3}$	$\frac{G(3M-4G)}{M-G}$	$M - 2G$	$G$	$\frac{M-2G}{2M-2G}$	$M$
$(\nu, M)$	$\frac{M(1+\nu)}{3(1-\nu)}$	$\frac{M(1+\nu)(1-2\nu)}{1-\nu}$	$\frac{M\nu}{1-\nu}$	$\frac{M(1-2\nu)}{2(1-\nu)}$	$\nu$	$M$

Note : the real and imaginary parts of the Poisson moduli  $\sigma$  may have any sign.

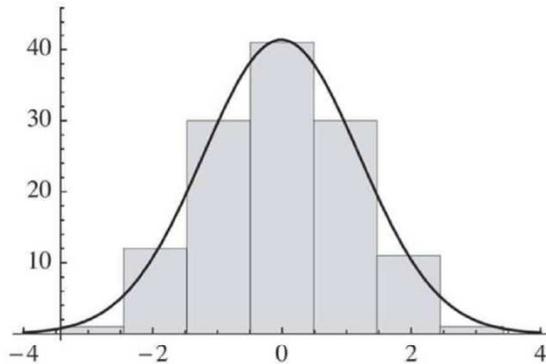
$$S = \pm\sqrt{E^2 + 9M^2 - 10EM}$$

$$R = \sqrt{E^2 + 9\lambda^2 + 2E\lambda}$$

# Ringdown Fitting Residuals

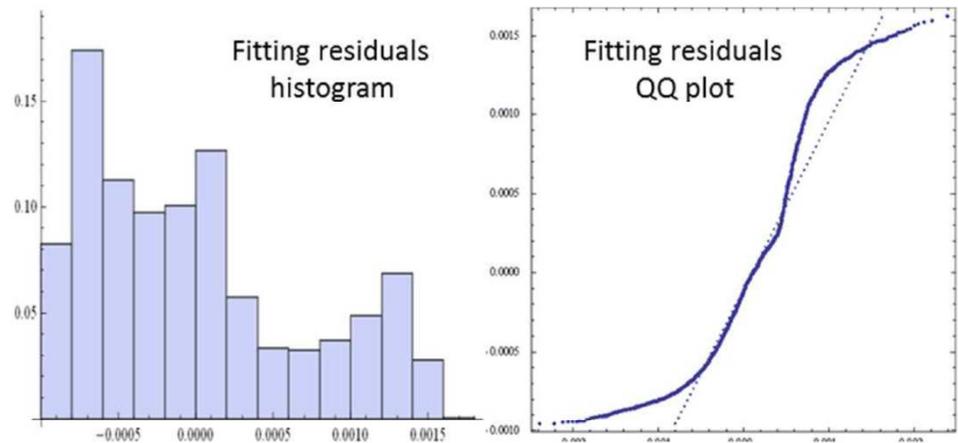
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Typical loss angle fitting residuals, TNI measurements



[Villar et al., PRD 81 (2010) ]

Typical loss angle fitting residual, clamped cantilever based ring-down measurement



[data courtesy N. Morgado (2008)]

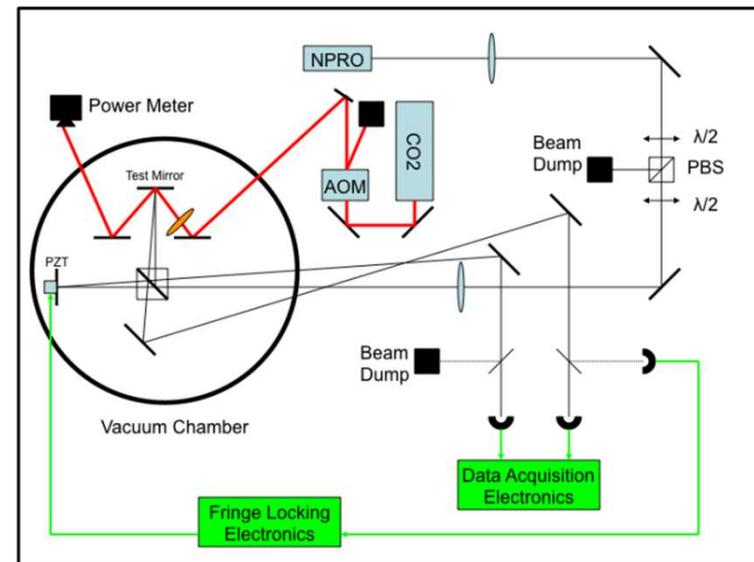
Confidence intervals must be robustly estimated in the non Gaussian case.

# Measuring Thermo-Optic Coefficients

Further coating thermal noise sources stem from thickness and index fluctuations driven by temperature fluctuations of thermodynamic (thermo-optic noise) or beam intensity related (photothermal noise) origin.

Coherent superposition of TE and TR fluctuations lead to quasi-cancellation in Silica/Tantala coatings.

Both TE and TR coeffs. are large in crystalline coating. Precise knowledge needed to exploit cancellation by proper design.



## Existing facilities:

- **Whitman College (G. Ogin)**

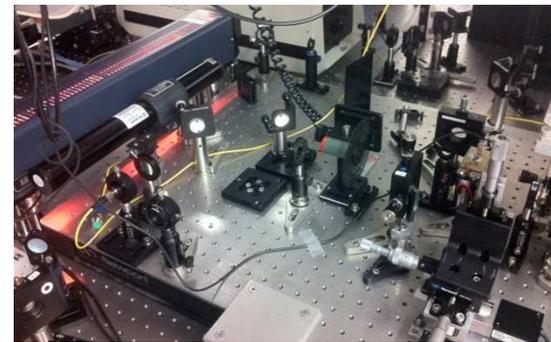
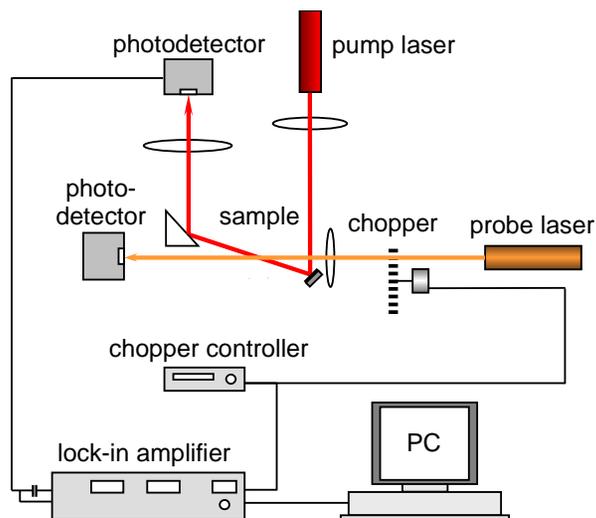
[Ogin et al., LIGO-P1600067]

# Measuring Optical Absorption

Need to measure optical absorption at sub-ppm level, below what is allowed by std ellipsometry. A few groups worldwide have adequate facilities, including

- **Stanford (M. Fejer)**
- **Glasgow (I. Martin)**
- **LMA (G. Cagnoli)**

- Photo-thermal Common-path Interferometry (PCI)
  - Measures bulk and coating absorptions
  - Cryo operation possible (15K)
  - Measures thermal lensing due to absorption
  - Sensitivity level (9 W beam ): 0.05 ppm/cm (coating), 0.2 ppm/cm and (bulk )



[Lasztko e al., Appl. Opt. 49 (2010) 5391]

# Outlook

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Why Coating R&D

Where are we now : the aLIGO mirrors

How can we progress:

- Improving Modeling
- Improving Processes
- Improving Characterization

Ongoing Studies & New Ideas:



- Nanolayered Composites
- Silicon Nitrides
- Crystalline Coatings
- M-ary Coatings
- Metamaterial Coatings

Conclusions

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# Nanolayered Composites

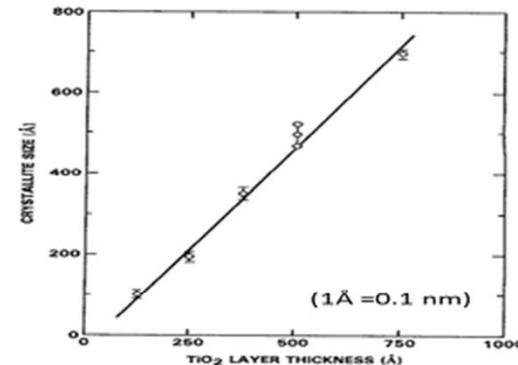
Seminal work on **thin – layer Titania** films by Sankur & Gunning [J. Appl. Phys. 66 (1989) 4747]

*“Thinner layers (< 250 Å) required higher temperatures [to crystallize]. 65 Å layer films exhibit diffraction only after annealing at 600°C.”*

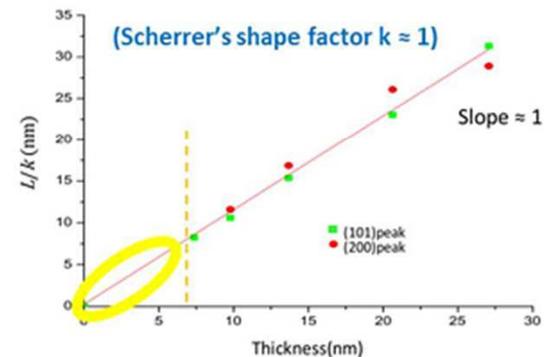
➔ ***“Grain size, as deduced from diffraction line broadening, was comparable to the layer thickness”***

*“Thicker layers remain in the Anatase phase and never transform into Rutile, even for prolonged (72 h) annealing at the highest temperatures (1100°C). Thinner layers (65 Å) convert into Rutile starting at 900°C”*

➔ ***“Below a certain critical thickness crystallization in pure TiO<sub>2</sub> films is inhibited”***

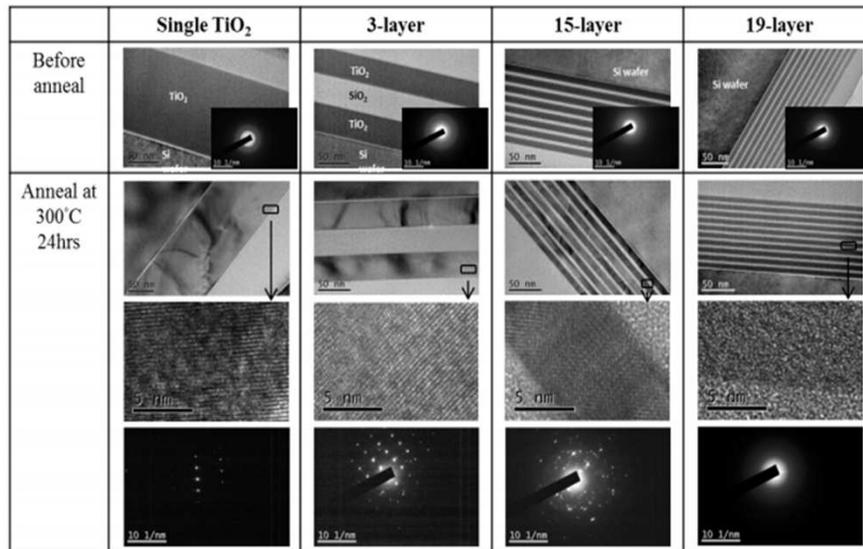


[Gluck et al., J. Appl. Phys. 69 (1991) 3037]

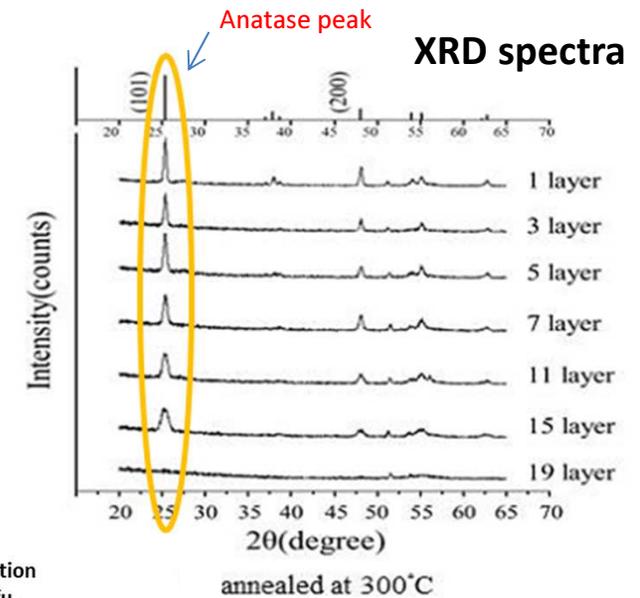


[S. Chao et al., LIGO-G1300921]

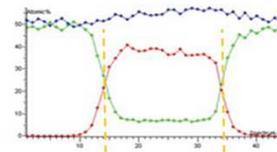
# Nanolayered Composites



All nanolayered composite prototype films :  
 $n_{eff} = 2.065$ , QWL thick @1064nm



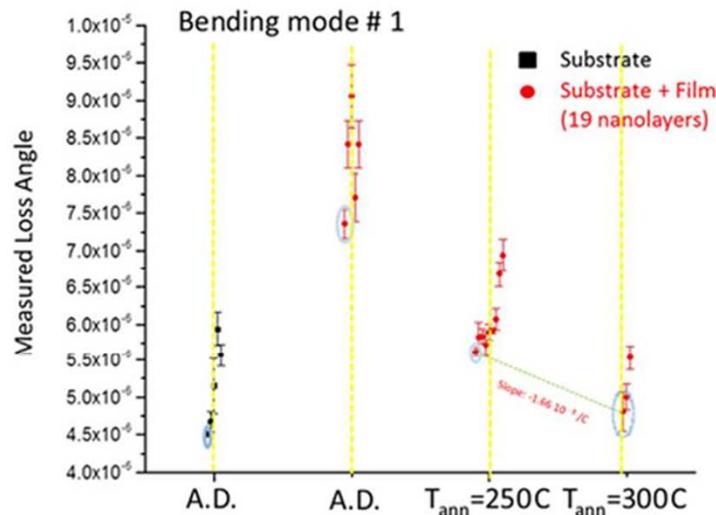
EDXRD investigation of interfacial diffusion before/after annealing (negligible)



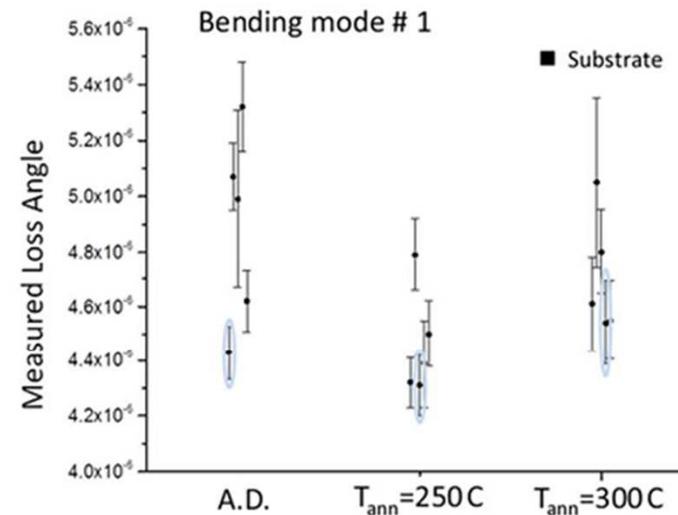
[Pan et al., Opt. Expr. **22** (2014) 29847]

# Nanolayered Composites

Loss angle of nm-layered composites reduces upon annealing (before crystallization) .  
 Losses of annealed composite better than those of Ti doped Tantalum (with same  $n$ )



Loss Angle		
$T_{ann}$	$\mu$	$\sigma/\mu$
A.D.	$7.36 \cdot 10^{-6}$	0.082
250	$5.64 \cdot 10^{-6}$	0.074
300	$4.81 \cdot 10^{-6}$	0.074
substrate + film (19 layers)		



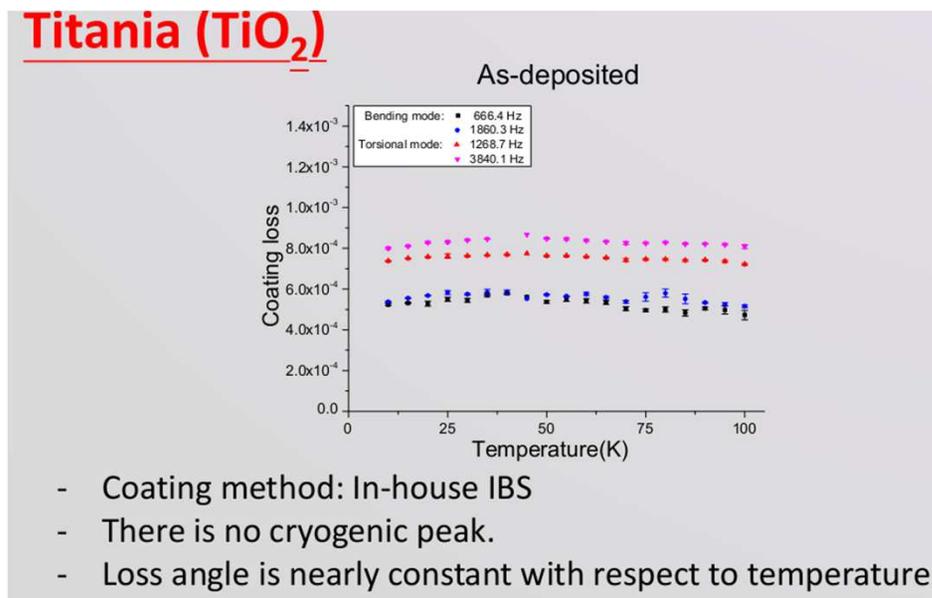
Loss Angle		
$T_{ann}$	$\mu$	$\sigma/\mu$
A.D.	$4.48 \cdot 10^{-6}$	0.073
250	$4.32 \cdot 10^{-6}$	0.044
300	$4.55 \cdot 10^{-6}$	0.046
substrate only (Silicon)		

[Chao et al., LIGO G1401055

# Nanolayered Composites

As a byproduct of nanolayered composite research, we confirmed the absence of a sensible cryopeak in Titania, much like in Hafnia.

[Chao et al, LIGO-G1601703]



Nanolayering makes It is possible to synthesize a variety of low loss, cryofriendly, crystallization resistant nanocomposite materials with an index ranging from 1.58 to 2.33.

## What remains TBD

- Optical loss measurement
- Effect of (many) interfaces on optical scattering
- How thin can nanolayers be ?

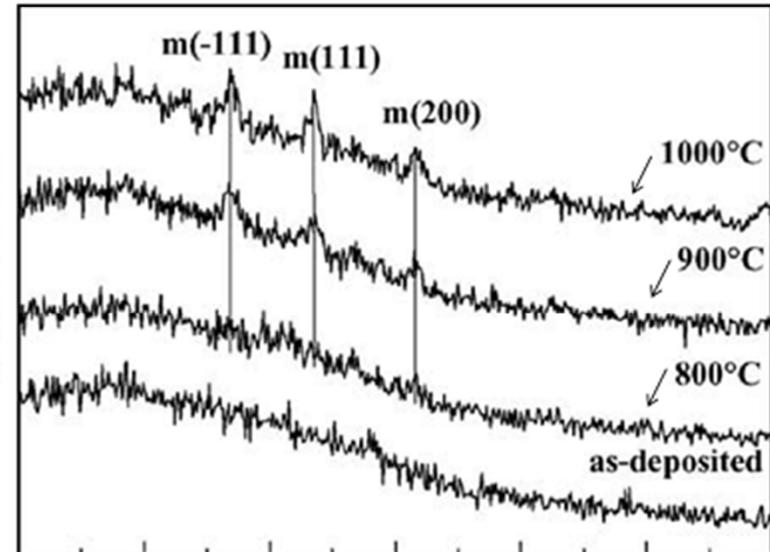
# Nanolayered Composites

**Nanometer-layered Hafnia (12nm)/Alumina (3nm) composites do not crystallize upon annealing, up to temperatures of 800 °C**

[M. Liu et al., Appl. Surf. Sci. 252 (2006) 6206].

“XRD analysis shows that the films remain amorphous up to an annealing temperature of 800 °C”

“FTIR indicates that no interface layer forms during annealing up to 800 °C”



# Outlook

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Why Coating R&D

Where are we now : the aLIGO mirrors

How can we progress:

- Improving Modeling
- Improving Processes
- Improving Characterization

Ongoing Studies & New Ideas:



- Nanolayered Composites
- **Silicon Nitrides**
- Crystalline Coatings
- M-ary Coatings
- Metamaterial Coatings

Conclusions

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# Silicon Nitrides

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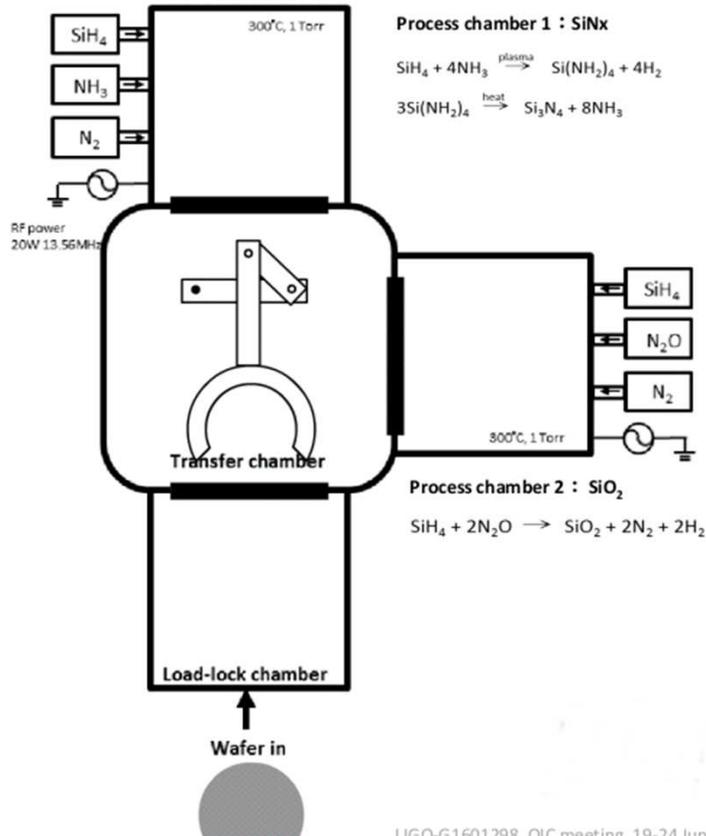
- $SiN_x$  obtained from PECVD.
- **Stoichiometry depends on deposition params** (gas flow rate, substrate temperature ( $x$  ranging from 0.40 to 0.87)). Larger  $x \rightarrow$  larger stresses in the film (120-420 Mpa). Higher stress  $\rightarrow$  lower mechanical losses (reduces TLS, and phonon coupling to them).
- **Refractive index can be fine tuned between 1.8 and 2.6.** Can be used for both low and high index material).
- **Mechanical loss angle at  $\sim 10^2 Hz$  below  $10^{-5}$ ; improves at cryo-temperatures. Extinction coefficient below  $10^{-3}$ .**

[Chao, Proc. Proc. OSA-OIC 2016, paper MB.12]

---

# Silicon Nitrides, contd.

## Chemical Vapor Deposition (CVD) for multi-layer dielectric mirror coating



SiN<sub>0.4</sub> /SiO<sub>2</sub> QW pairs deposited by all-CVD process show room temperature mechanical loss  $\sim 10^{-5}$ , lower than Ta<sub>2</sub>O<sub>5</sub> -TiO<sub>2</sub> /SiO<sub>2</sub> in current GW detector.

	2-layer	4-layer
High stress (measured)	$(4.42 \pm 1.83) \times 10^{-5}$	$(9.28 \pm 0.55) \times 10^{-5}$

[Chao et al, LIGO G1601298]

# Outlook

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Ongoing Studies & New Ideas:

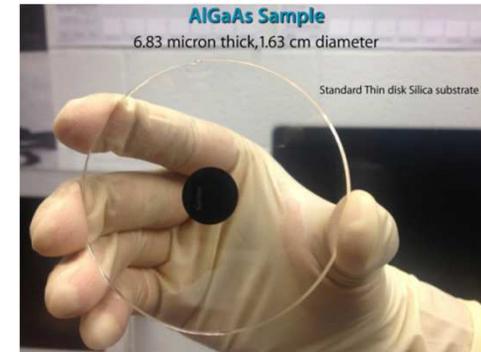
- Nanolayered Composites
- Silicon Nitrides
- Crystalline Coatings
- M-ary Coatings
- Metamaterial Coatings



Conclusions

# Crystalline Coatings (GaAs/AlGaAs, GaP, AlGaP)

- GaAs/AlGaAs - Strain noise level may be reduced by a factor  $\sim 3$  compared to current aLIGO; no cryo peak; better at lower T [Cole et al., Nat. Phot. 7 (2013) 644]. Very low optical (absorption & scattering) losses (at ppm levels for aLIGO design) [Cole et al., Optica 3 (2016) 647; see also Steinlechner et al., LIGO-G1401032; Singh, LIGO-G1501132]. **Must be transferred & bonded to substrate.**
- GaP/AlGaP - Coating *lattice-matched to crystalline Silicon* test mass ( $\rightarrow$  operation @1550nm) [Lin et al., Opt. Mater. Express, 5 (2015) 1890] Strain noise level reduced by a factor  $\sim 5$  compared to current aLIGO; no cryo peak [Cumming et al., CQG 32 (2015) 035002]. **Unsuitable for room temperature operation (large TE noise**



# Both GaAs/AlGaAs and GaP/AlGaP

---

## Technology Challenges

- Insufficient size for MBE grown c-coatings (as of today).
  - Upscaling (GaP/AlGaP) to  $\sim 40\text{cm } \varnothing$  ?
  - Tiling (GaAs/AlGaAs)  $\rightarrow$  Adhesion issues, curvature; edge scattering ?
- *oval defects* observed in MBE grown films  $\rightarrow$  scattering ?  
[Szerling et al. , Opt. Appl. XXXV (2005) 537]

## Modeling Issues (poorly investigated so far)

- AlGaAs and AlGaP are III-V compounds w. cubic cell (“zinc-blende”)  $\rightarrow$  optical & viscoelastic *anisotropy*
  - Nonlinear optical (Pockels, Kerr, free-carrier) effects
- } Impact on noise ?
- [Abernathy et al. LIGO T1400340; T1400276, T1500268, T1500357]

# Outlook

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Conclusions

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# Ternary (m-ary) Coatings

[Steinlechner et al., PRD 91 (2015) 069904]

[Yam et al., PRD 91 (2015) 042002]

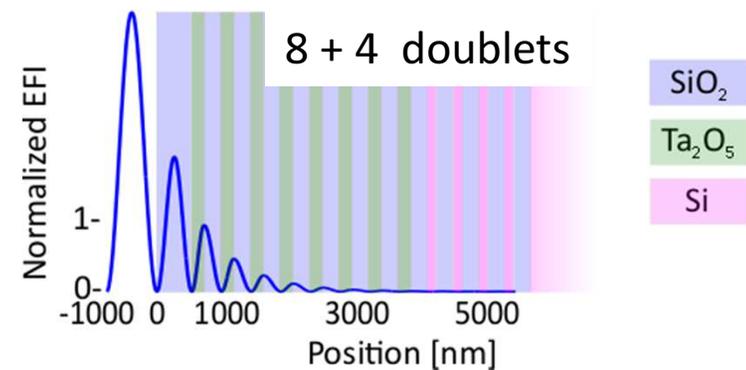
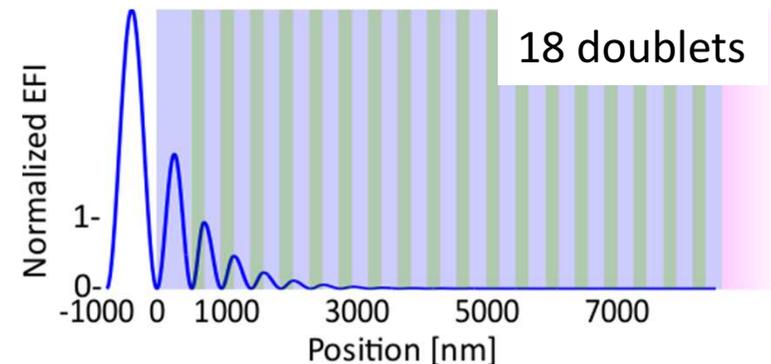
Use optically dense(r) but lossy(er) materials in the bottom layers, where field is weak(er).

Fewer doublets;

Thinner coating, lower TN

TBD

- Thickness optimization;
- Effect on spectral response of different material chromatic dispersion ;



[20% TN reduction at 25C]

# Outlook

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Conclusions

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# Mie MM Mirror

---

In the spectral bands where the permeability *or* the permittivity of the Mie MM is negative (*not* both), the effective characteristic impedance of the composite is imaginary ( $Z = \iota X$ , *pure reactance*), as well as its propagation constant ( $\beta = -\iota|\beta|$ , *evanescent wave*).

Under such circumstances, the reflectance of a Mie-MM-filled halfspace is

$$R = \left| \frac{\iota X - Z_0}{\iota X + Z_0} \right|^2 = 1$$

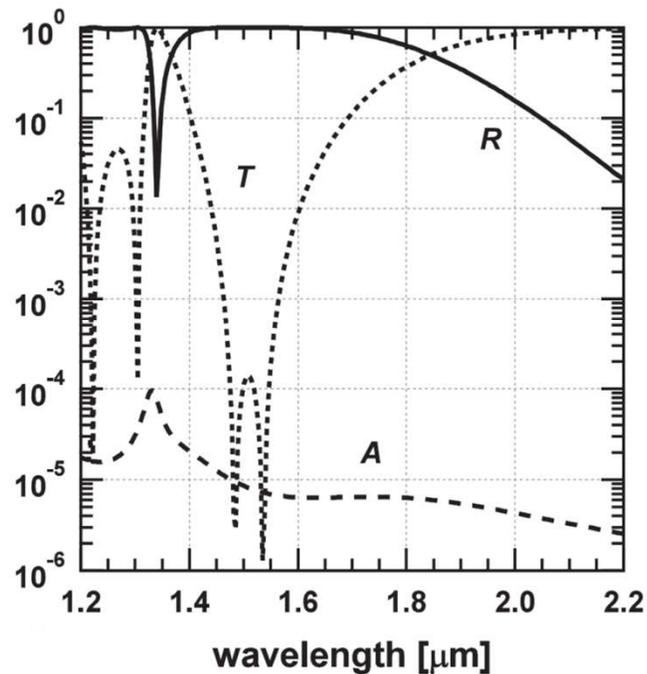
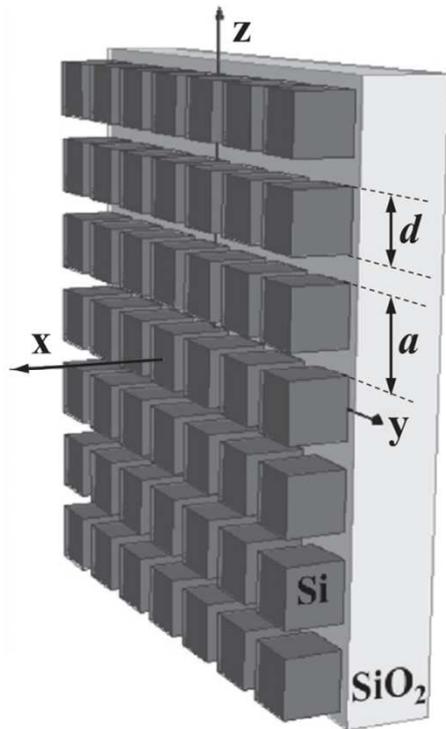
and the extinction length in it is  $|\beta|^{-1}$ .

➔ **Ideally, the above properties could allow to design a perfect ( $R = 1$ ) and thin ( $|\beta| \gg 1$ ) mirror ...**

---

# Example (Numerical)

Numerical simulation (CST<sup>®</sup> commercial code)



Silicon on Siica  
(losses included)

$$d = 450 \text{ nm}$$
$$a = 670 \text{ nm}$$

Transmittance  
& absorbance  
below  $10^{-5}$

[Slovick et al., Phys. Rev. B88 (2013) 165116]

# Mie-MM Mirror Feasibility (2017)

*Best method as of 2017* in terms of accuracy in nanoparticle (nano-cylinder) size /placement

- e-beam lithography
- reactive-ion etching
- filler deposition

Silicon on Silica or Alumina;  $\text{Si}_3\text{N}_4$  filler

[Staude et al., ACS nano, 7 (2013) 7824]

⋮

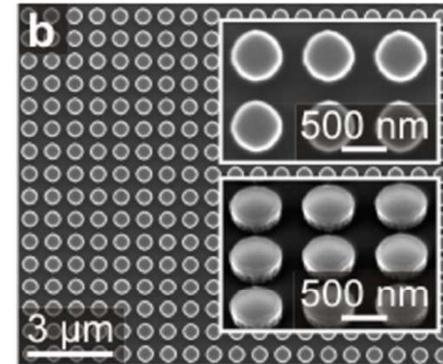
*Cheapest* (and worst in terms of process control)

- Colloidally self-assembly mask
- ...

[Chang et al., ACS Nano Lett. 11 (2011) 2533]

➔ Scalability poses no problem

See e.g. [Krasnok et al., Proc. SPIE 9502 (2015) 950203] for a review



Electron microscopy Image of prototype  
[Staude, et al.]

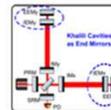
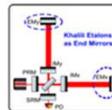
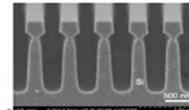
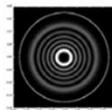
# More Coating R&D

keyword	year	selected reference(s)	Status
Thickness Optimization	2005	LIGO G050176 (2005) ... PRD 81 (2010) 122001	<i>AdLIGO baseline design</i>
Doped Tantalum	2007	Class. Quantum Grav. 24 (2007) 405 ...	<i>AdLIGO baseline design</i>
Cryogenic Coatings	1999	Int. J. Mod. Phys. D8 (1999) 557 ... Opt. Lett. 38(2013) 5268	R&D
"Wide" (or HOGL) beams	2003	PRD 67 (2003) 102004 ... CQG 30 (2013) 035004	R&D
Khalili's Resonator and "Etalon"	2004	Phys. Lett. A334 (2004) 67, Phys. Lett. A375 (2011) 4147	R&D
Coating-less Mirrors	2004	Phys Lett A324 (2004) 345,..., PRD 76 (2007) 053810	R&D
Diffractive "Mirrors"	2006	CQG 23 (2006) 7297 ... LIGO P-1300034 (2013)	R&D
Crystalline Coatings	2012	LIGO G1200948 (2012) ... Nature Phot. 7 (2013) 644	R&D

So far, only doped Tantalum and thickness-optimization progressed to the production stage (and became part of the AdLIGO baseline design).

Most of the above (clever) ideas are still facing *major technological challenges*.

Will nm-layered composites be a viable route ?



# Outlook

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Why Coating R&D

Where are we now : the aLIGO mirrors

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Ongoing Studies & New Ideas:

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 Conclusions

# Conclusions

---

Reducing coating thermal noise is mandatory to improve the performance of interferometric detectors of GW.

We need well understood, reliable, repeatable protocols to measure coating-relevant material parameters;

We need a better understanding/control of *the Physics* behind the coating (noise) properties;

We need to explore in depth better depositions, smart doping, nanolayered composites, M-ary coating; crystalline coatings and maybe Mie Metamaterials;

**We need young talented scientists to work on such issues (and money to keep them alive).**

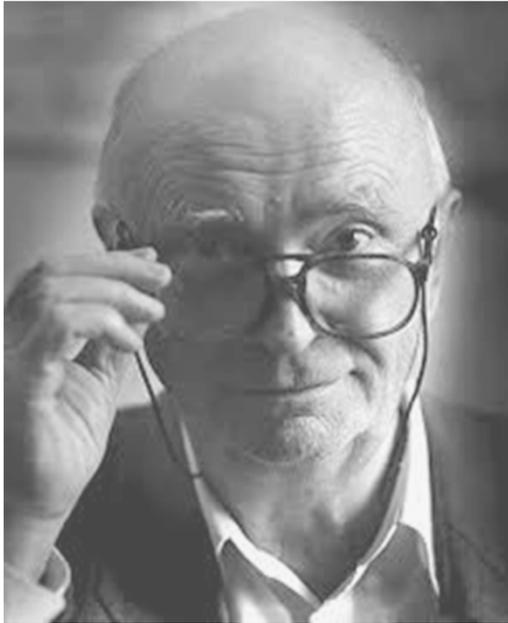
# Acknowledgements

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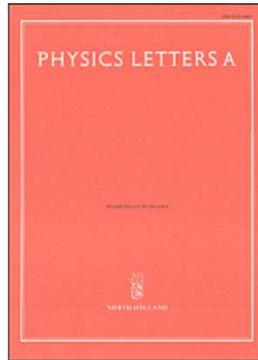
This work has been sponsored in part by the EU through the EU-FP-7 ELiTES (IRSES) Project; by the Italian National Institute for Nuclear Physics (INFN, CSN - 5) under the COAT, MidiBRUT and AdCOAT grants; by the National Science Council of Taiwan under NSC-1002221-E-007-099.

# Honoring a Master

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Vladimir Borisovich Braginsky  
(3/8/1931-30/3/2016)



## Special Issue:

- Low-dissipation systems,
- Noise and fluctuations,
- Quantum-limited and QND measurements,
- Macroscopic Quantum Mech.,
- Optomechanical effects,
- Optical / microwave whispering gallery modes,
- GW detectors,
- Selected aspects of Gravitation Physics (spin-quadrupole effect, equivalence principle, etc.)



**Submission Deadline : March 17<sup>th</sup> 2017**

<https://www.journals.elsevier.com/physics-letters-a/call-for-papers/special-issue-in-memory-of-prof-vladimir-borisovich-braginsky>

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# Mie Metamaterials Coatings

# Metamaterials (MMs)

---

From the Greek noun μετά (beyond) is, at large, an artificially engineered material with properties that aren't found in any known natural material.

Historically, meant to denote materials whose dielectric permittivity and/or magnetic permeability is *negative* in some spectral band [Veselago, Sov. Phys. Usp. 10 (1968) 509].

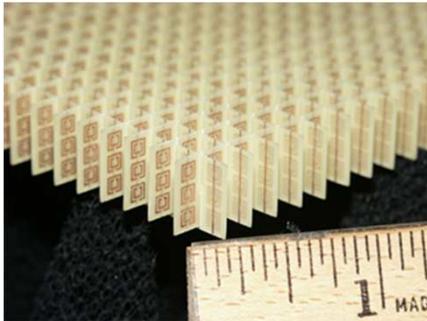
Conceptual extension to mechanical constitutive properties (bulk modulus, density) with applications in Acoustics, Structural Engineering, etc., followed.

At the core of the US-DoD **Multidisciplinary University Research Initiative** (MURI), and the UE **Metamorphose** Research Network.

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# MMs, contd.

---



First working metamaterial demonstrated in 2001 [Shelby et al., Science 292 (2001)], based on lattices of split-ring resonators and metallic wires [Smith et al., PRL 84 (2000) 4184] working in the GHz range...

Paved the way to unforeseen new apps including e.g. *super-resolution imaging* [Grbic & Eleftheriades PRL 92 (2004) 117403] and *invisibility cloaking* [Shurig et al., Science. 314 (2006) 5801], that were steadily improved during the subsequent decade;

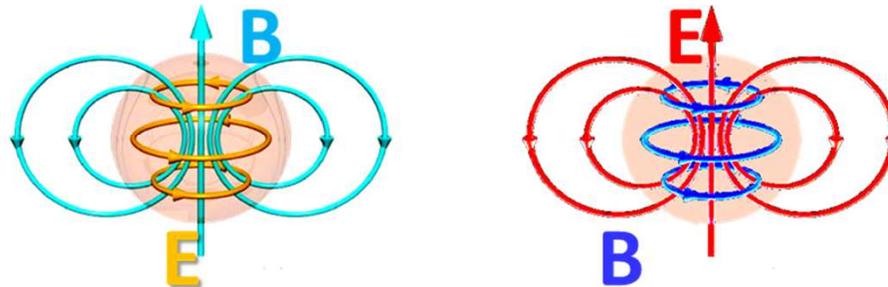
Scaling to optical frequencies initially hindered by large losses in metals; made possible by exploiting Mie resonance in dielectric nanosphere arrays [O'Brien & Pendry, J. Phys. Cond. Matt. 14 (2002) 6383].

# Mie MMs in a Nutshell

---

The spherical multipole expansion of the EM field scattered by a sphere was first derived by Gustav Mie [Ann. Phys. 330 (1908) 377] in terms of spherical Bessel functions.

The scattering coefficients exhibit *resonances*, known as *Mie resonances* [Uslenghi, *Electromagnetic Scattering*, Acad Press, 1978]



Lowest order (dipole) Mie resonances - Left: magnetic; right: electric

The resonant wavelengths depend on the radius and dielectric contrast of the sphere. For a Si sphere in air, with  $d = 0.25\mu$ , e.g., the lowest electric and magnetic resonances occur at  $\lambda \approx 1.2\mu$  and  $\lambda \approx 1.7\mu$

# Mie MMs in a Nutshell, contd.

The effective permittivity and permeability of a *lattice of spheres in a host medium* was first computed by Lewin [Lewin, Proc. IEE, 94 (1947) 65]

$$\varepsilon_{eff} = \varepsilon_h \left( 1 + \frac{3\eta}{\frac{F(\xi) + 2(\varepsilon_h/\varepsilon_s)}{F(\xi) - (\varepsilon_h/\varepsilon_s)} - \eta} \right), \quad \mu_{eff} = \mu_h \left( 1 + \frac{3\eta}{\frac{F(\xi) + 2(\mu_h/\mu_s)}{F(\xi) - (\mu_h/\mu_s)} - \eta} \right)$$

where:

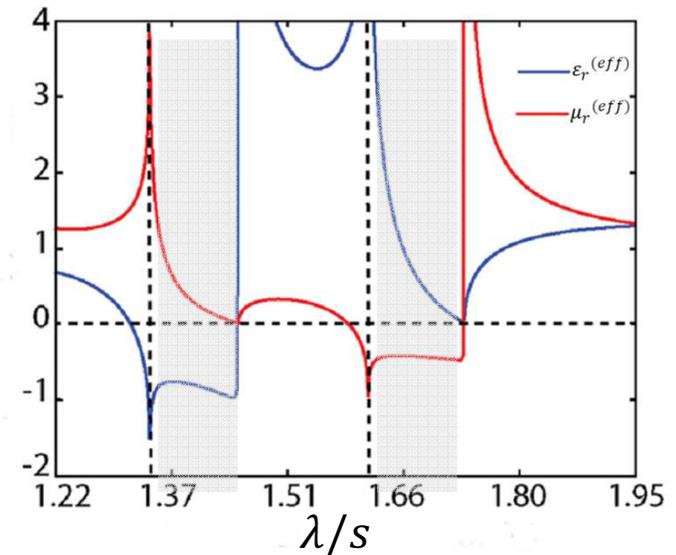
$\eta$  = volume fraction of spheres;

$$F(\xi) = \frac{2(\sin \xi - \xi \cos \xi)}{(\xi^2 - 1)\sin \xi + \xi \cos \xi}$$

$\xi = \omega \sqrt{\varepsilon_s \mu_s} R_s$ ,  $R_s$  = radius of spheres

$(\varepsilon_h, \mu_h)$  = permittivity & permeab. of host

$(\varepsilon_s, \mu_s)$  = permittivity & permeab. of spheres



➔ Featuring  $Re[\varepsilon] < 0$  or  $Re[\mu] < 0$  in some bands (SNG-MM)

# Mie MM Mirror

---

In the spectral bands where the permeability *or* the permittivity of the Mie MM is negative (*not* both), the effective characteristic impedance of the composite is imaginary ( $Z = \iota X$ , *pure reactance*), as well as its propagation constant ( $\beta = -\iota|\beta|$ , *evanescent wave*).

Under such circumstances, the reflectance of a Mie-MM-filled halfspace is

$$R = \left| \frac{\iota X - Z_0}{\iota X + Z_0} \right|^2 = 1$$

and the extinction length in it is  $|\beta|^{-1}$ .

 **Ideally, the above properties could allow to design a perfect ( $R = 1$ ) and thin ( $|\beta| \gg 1$ ) mirror ...**

# Lossy Mie-MM Mirror

The (normal incidence, plane wave) reflection coefficient of a SNG MM ( $Re[\varepsilon]Re[\mu] < 0$ ) in vacuum can be written

$$\Gamma = \frac{\frac{Z_{MM}}{Z_0} - 1}{\frac{Z_{MM}}{Z_0} + 1} = \frac{Re[\bar{Z}_{MM}] - 1 + jIm[\bar{Z}_{MM}]}{Re[\bar{Z}_{MM}] + 1 + jIm[\bar{Z}_{MM}]} \quad R = |\Gamma|^2 = \frac{(Re[\bar{Z}_{MM}] - 1)^2 + (Im[\bar{Z}_{MM}])^2}{(Re[\bar{Z}_{MM}] + 1)^2 + (Im[\bar{Z}_{MM}])^2}$$

For small losses,  $|Im[\varepsilon]| \ll |Re[\varepsilon]|$  and  $|Im[\mu]| \ll |Re[\mu]|$

$$\bar{Z}_{MM} = \pm \sqrt{\frac{\varepsilon_0}{\mu_0} \left| \frac{Re[\mu]}{Re[\varepsilon]} \right|} \left[ j - \frac{\delta}{2} \right], \quad \delta = \frac{Im[\varepsilon]}{Re[\varepsilon]} - \frac{Im[\mu]}{Re[\mu]}$$

Hence

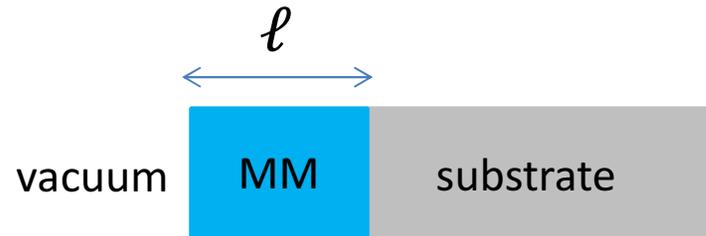
$$R = 1 - \frac{2 \sqrt{\frac{\varepsilon_0}{\mu_0} \left| \frac{Re[\mu]}{Re[\varepsilon]} \right|}}{1 + \frac{\varepsilon_0}{\mu_0} \left| \frac{Re[\mu]}{Re[\varepsilon]} \right|} |\delta|$$

Can be made small at will using *low-loss dense materials*

# Finite Thickness Mie-MM Mirror

---

After some lengthy but obvious algebra (reflection coefficient transport equation), under the assumption that both both reflectances  $R_{1,2}$  at the vacuum-MM and MM-substrate interfaces are close to unity ,



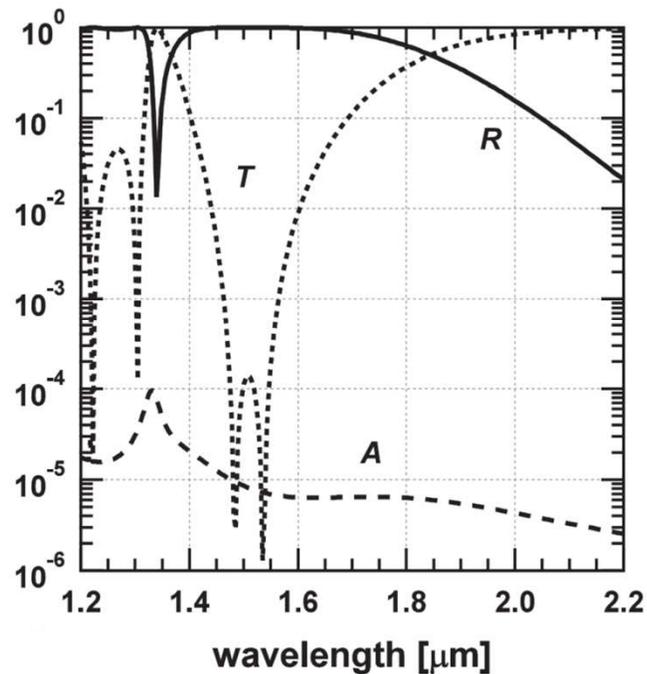
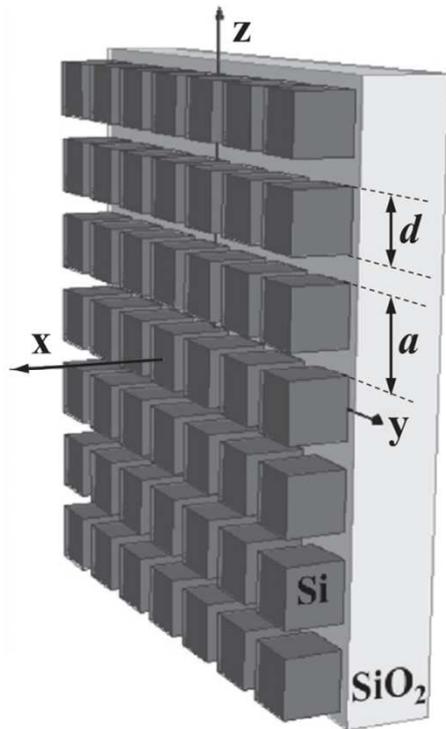
$$R_{1,2} = 1 - \delta_{1,2} , \text{ with } \delta_1 \sim \delta_2 \sim \delta \ll 1$$

It is found that for a finite-thickness MM layer

$$R_\ell = R_\infty - \delta_\ell , \text{ with } \delta_\ell \leq 2 \exp \left( - \frac{4\pi\ell}{\lambda_0} \sqrt{\frac{|Re[\varepsilon]Re[\mu]|}{\varepsilon_0\mu_0}} \right)$$

# Example (Numerical)

Numerical simulation (CST<sup>®</sup> commercial code)



Silicon on Siica  
(losses included)

$$d = 450 \text{ nm}$$
$$a = 670 \text{ nm}$$

Transmittance  
& absorbance  
below  $10^{-5}$

[Slovick et al., Phys. Rev. B88 (2013) 165116]

# Thermal Noise of MM Coating

---

For practical purposes, the viscoelastic properties of a Mie-MM can be computed using *effective medium theory* [Principe et al., *Phys. Rev. D*91 (2015) 022005].

The MM-film can be one order of magnitude thinner than a traditional (multilayer, Bragg) coating with equivalent reflectance. We may naively expect a comparable ratio (one order of magnitude) in thermal noise PSD.

A rigorous ab-initio thermal noise calculation can be worked out paralleling the analysis in [Heinert et al., *Phys. Rev. D*88 (2013) 42001] for grating reflectors (Pinto et al., work in progress).

# Mie-MM Mirror Feasibility (2017)

*Best method as of 2017* in terms of accuracy in nanoparticle (nano-cylinder) size /placement

- e-beam lithography
- reactive-ion etching
- filler deposition

Silicon on Silica or Alumina;  $\text{Si}_3\text{N}_4$  filler

[Staude et al., ACS nano, 7 (2013) 7824]

⋮

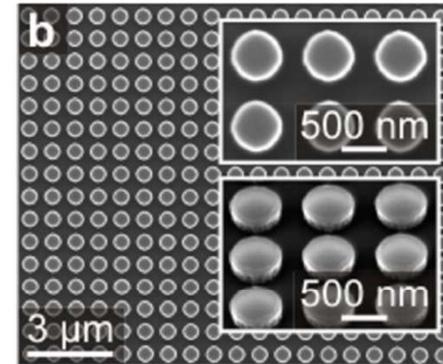
*Cheapest* (and worst in terms of process control)

- Colloidally self-assembly mask
- ...

[Chang et al., ACS Nano Lett. 11 (2011) 2533]

➔ Scalability poses no problem

See e.g. [Krasnok et al., Proc. SPIE 9502 (2015) 950203] for a review



Electron microscopy Image of prototype [Staude, et al.]

# *New Ideas May be Hard to Receive ... but Worth a Try !*

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